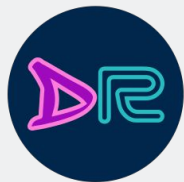


ROB 498/599: Deep Learning for Robot Perception (DeepRob)

Lecture 20: 3D Vision Techniques; Nerf

03/31/2025



<https://deeprob.org/w25/>

Today

- Feedback and Recap (5min)
- 3D Shape Representations (40min)
- NeRF (25min)
- Summary and Takeaways (5min)

Tomorrow

Tuesday April 1, 2025

Starts 3:30pm EST @CSRB 2246

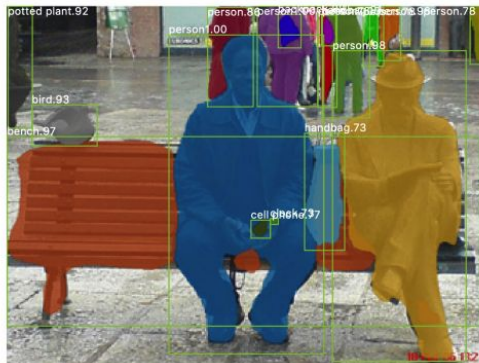
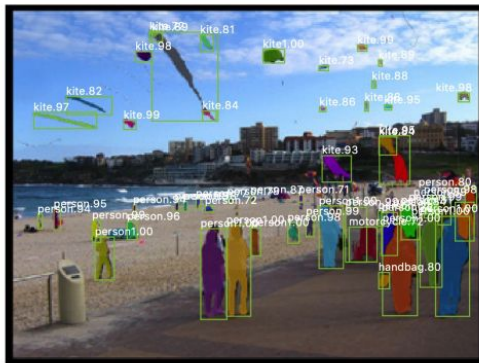
5min “lightning talk” - final project proposal presentations

- All group members must speak
- Upload presentation files to [Final Project LightningTalk folder](#) on Google Drive by April 1st 3:30pm EST
- We will go by group number order
- 5% grade

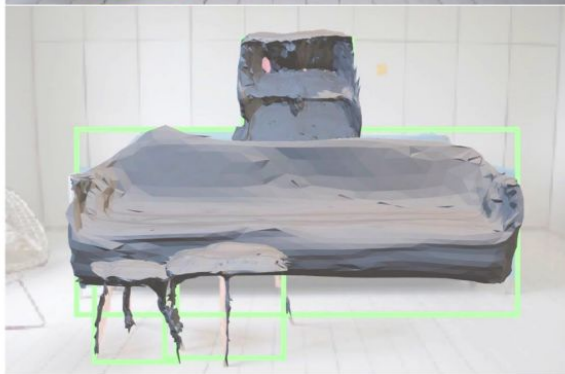
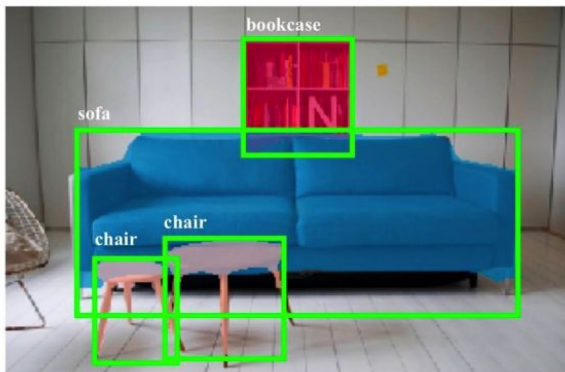
3D Shape Representations

Previously... Predicting 3D Shapes of Objects

Mask R-CNN:
2D Image -> 2D shapes



Mesh R-CNN:
2D Image -> 3D shapes



He, Gkioxari, Dollár, and Girshick, "Mask R-CNN", ICCV 2017

<https://arxiv.org/abs/1703.06870>

Gkioxari, Malik, and Johnson, "Mesh R-CNN", ICCV 2019

https://openaccess.thecvf.com/content_ICCV_2019/papers/Gkioxari_Mesh_R-CNN_ICCV_2019_paper.pdf

Also recall... "Speech2Mesh"

"Cartoon picture of a baby dinosaur with wings"



Image generated from
Dall-E 2



Multiview images
generated through
Diffusion Model



Generated Mesh

<https://deeprob.org/w24/reports/speech2mesh/>

DeepRob W24
Project

(Adeshara et al.)

"A Round ceramic cup with the handle of an elephant "



Image generated from
Dall-E 2



Multiview images
generated through
Diffusion Model



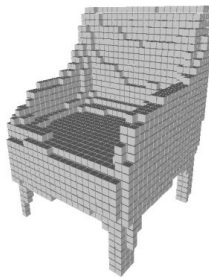
Generated Mesh

Today

Predicting 3D Shapes
from single image

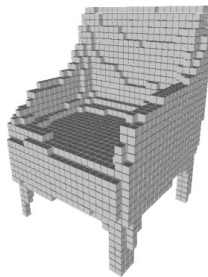


Input Image



3D Shape

Processing 3D
input data



3D Shape



Chair

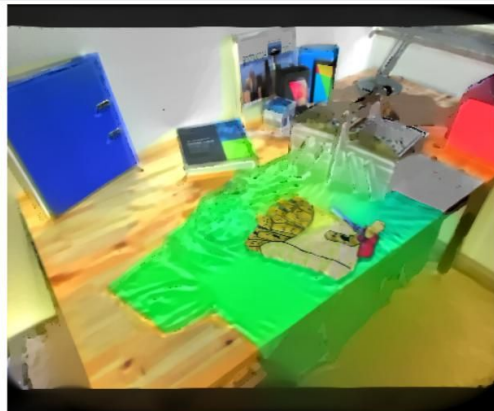
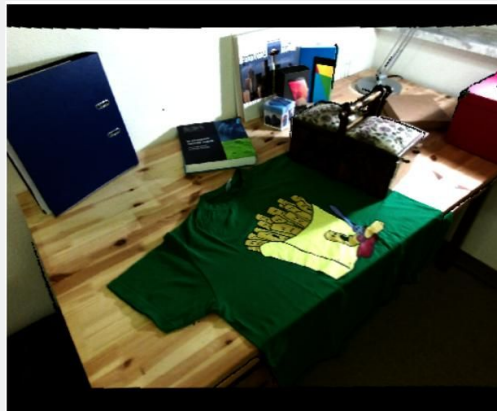


More topics in 3DV:

- Computing correspondences
- Multi-view stereo Structure from Motion
- Simultaneous Localization and Mapping (SLAM)
- Self-supervised learning
- Differentiable graphics
- 3D Sensors

<https://3dvconf.github.io/2025/>
(3DV)
<https://s2025.siggraph.org/>
(SIGGRAPH)

3D data modalities



<https://www.nist.gov/image/hyperspectralcube4501png>

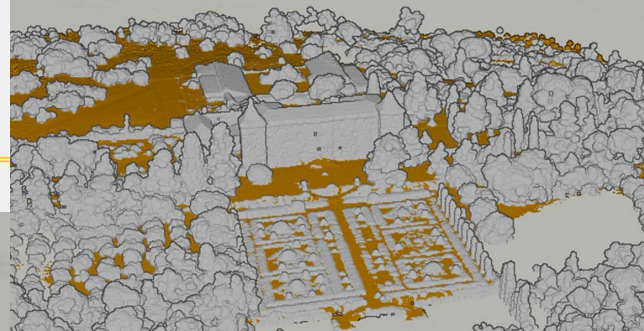
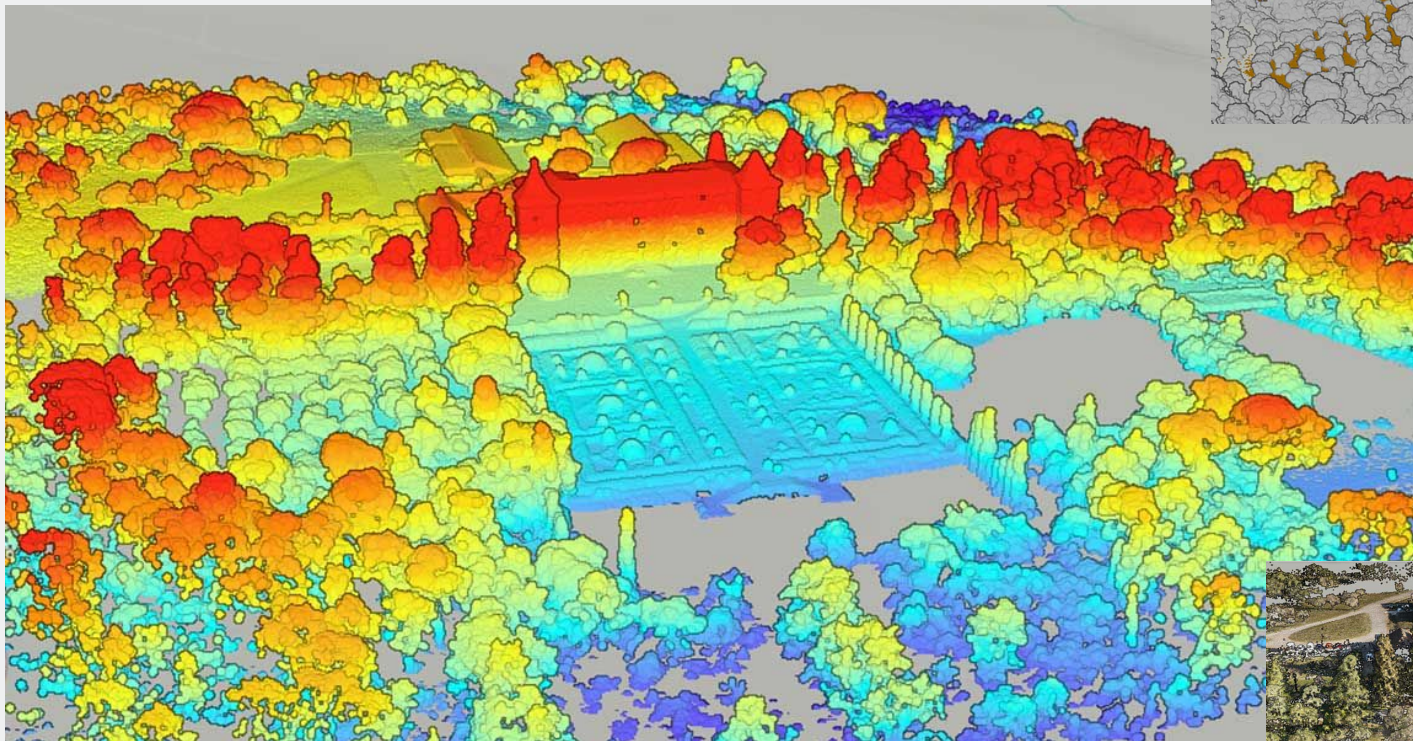
https://www.flir.com/oem/adas/adas-dataset-form/?srsltid=AfmBOoovTeVL1G2vPoiodz5G9ciTWsL_18DTQSWGiuV5qXcCW_Xr2q39S



RGB-T
(thermal)

<https://paperswithcode.com/dataset/tum-rgb-d>

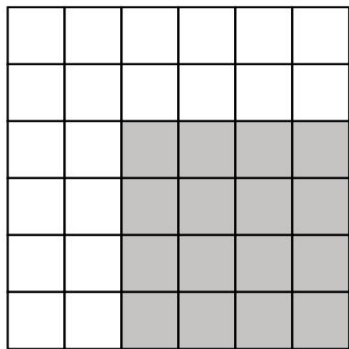
3D data modalities



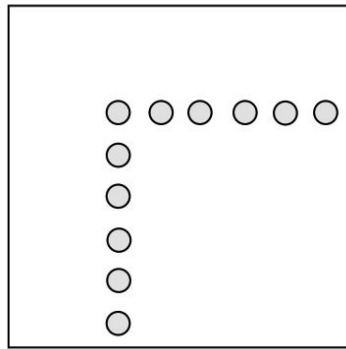
3D Shape Representations



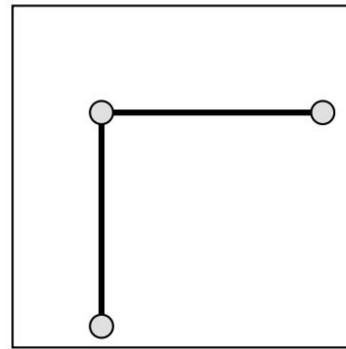
Depth
Map



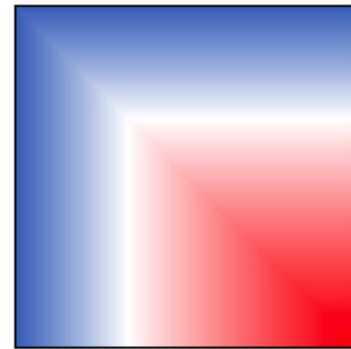
Voxel
Grid



Pointcloud



Mesh



Implicit
Surface

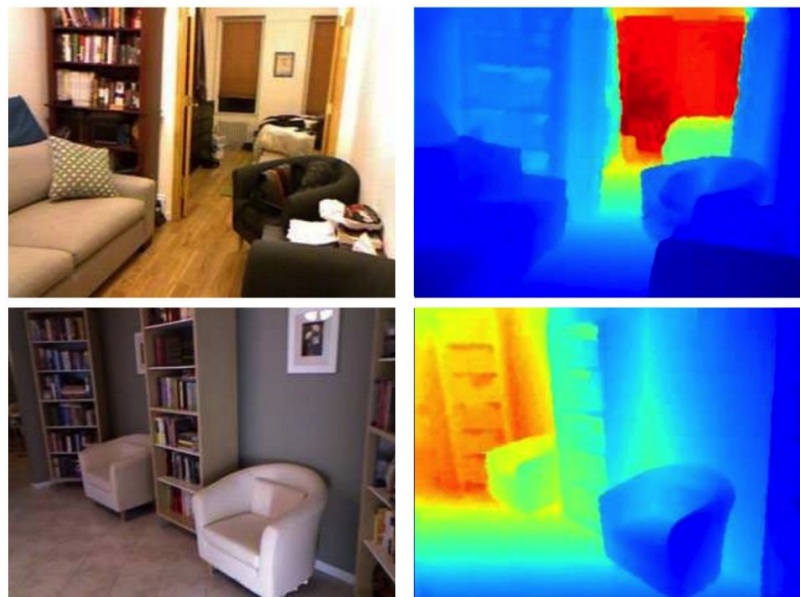
3D Shape Representations

Q: Why 2.5D?

For each pixel, **depth map** gives distance from the camera to the object in the world at that pixel

RGB image + Depth image
= RGB-D Image (2.5D)

This type of data can be recorded directly for some types of 3D sensors (e.g. Microsoft Kinect)



RGB Image: $3 \times H \times W$ Depth Map: $H \times W$

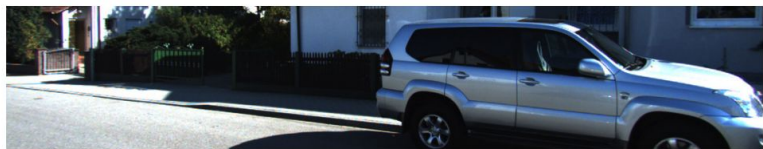
https://openaccess.thecvf.com/content_iccv_2015/papers/Eigen_Predicting_Depth_Surface_ICCV_2015_paper.pdf

Predicting Depth Maps

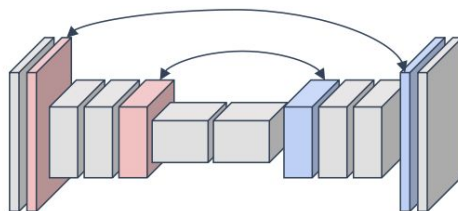
(KITTI dataset)

https://papers.nips.cc/paper_files/paper/2014/hash/91c56ce4a249fae5419b90cba831e303-Abstract.html

<https://www.cvlibs.net/datasets/kitti/>



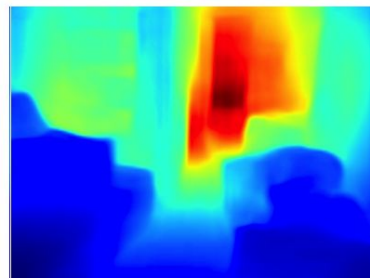
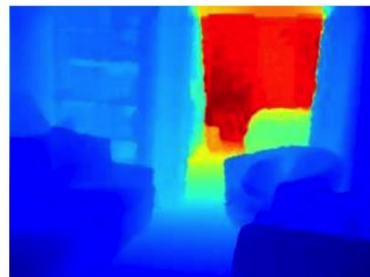
RGB Input Image:
 $3 \times H \times W$



**Fully Convolutional
network**

Predicted Depth Image:

$1 \times H \times W$



**Per-Pixel Loss
(L2 Distance)**

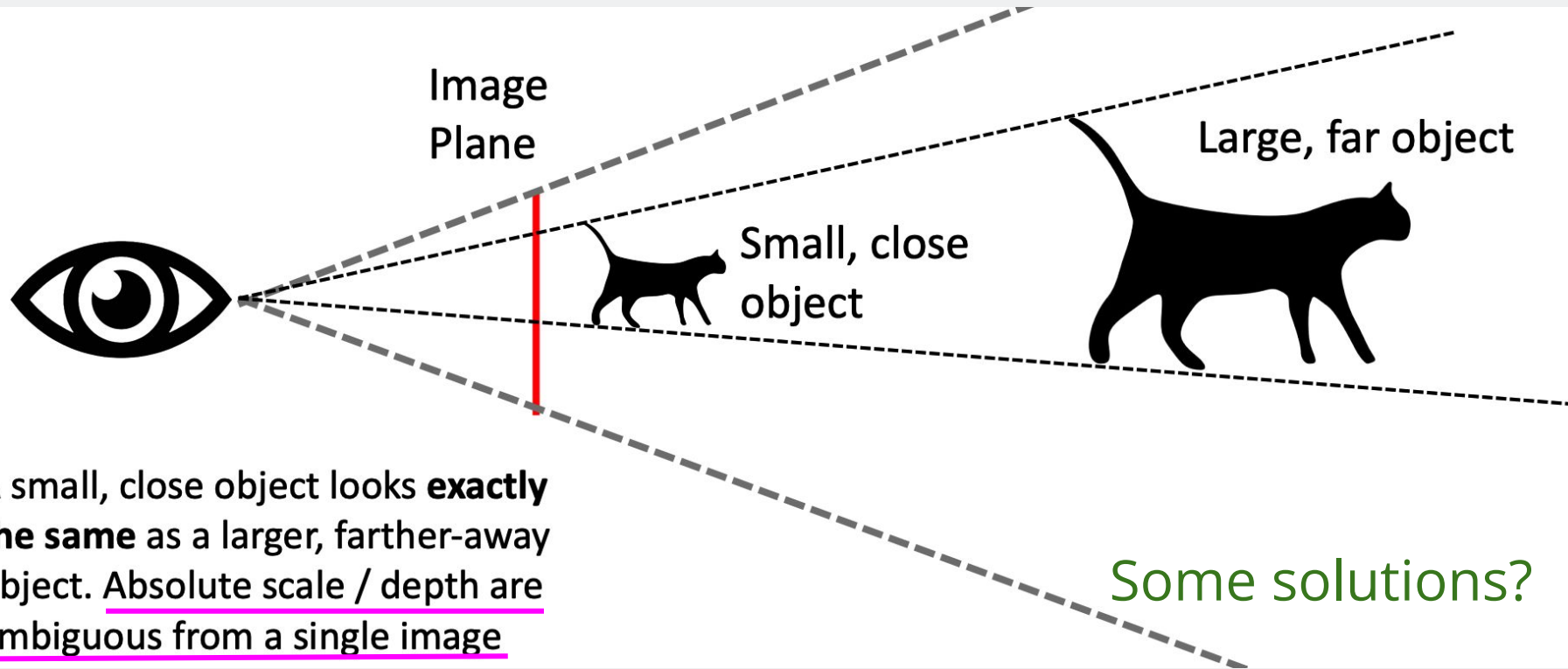
Predicted Depth Image:
 $1 \times H \times W$

Aha Slides (In-class participation)

<https://ahaslides.com/YSRO4>



Problem: Scale / Depth Ambiguity



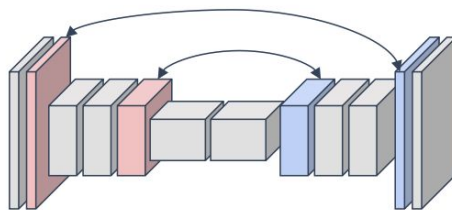
Predicting Depth Maps

Scale-invariant mean squared error
(in log space)

$$\begin{aligned} D(y, y^*) &= \frac{1}{2n^2} \sum_{i,j} ((\log y_i - \log y_j) - (\log y_i^* - \log y_j^*))^2 \\ &= \frac{1}{n} \sum_i d_i^2 - \frac{1}{n^2} \sum_{i,j} d_i d_j = \frac{1}{n} \sum_i d_i^2 - \frac{1}{n^2} \left(\sum_i d_i \right)^2 \end{aligned}$$



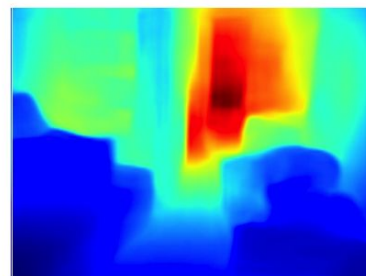
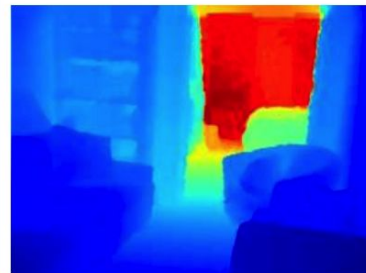
RGB Input Image:
3 x H x W



**Fully Convolutional
network**

Predicted Depth Image:

1 x H x W



**Per-Pixel Loss
(Scale invariant)**

3D Shape Representations: Surface Normals

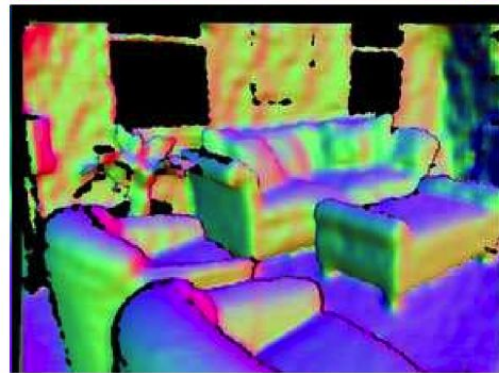
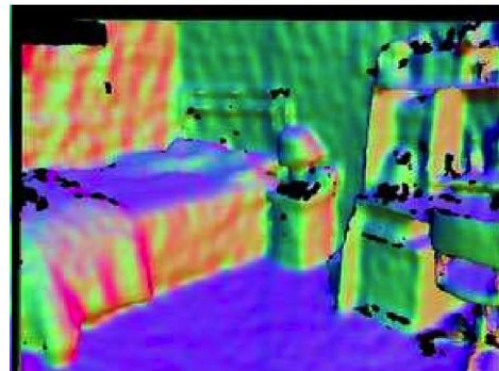
For each pixel, **surface normals** give a vector giving the normal vector to the object in the world for that pixel

Q: How to obtain surface normals?

<https://arxiv.org/pdf/1411.4734>



RGB Image: $3 \times H \times W$

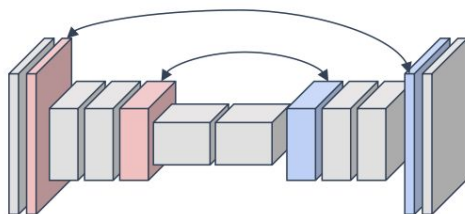


Normals: $3 \times H \times W$

Predicting Surface Normals



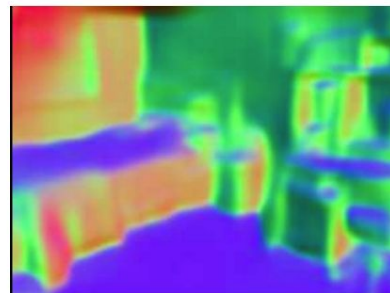
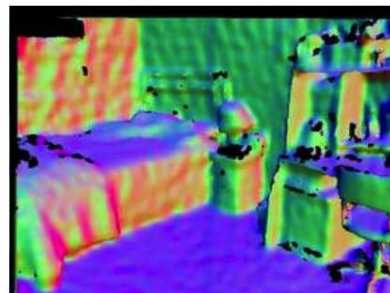
RGB Input Image:
 $3 \times H \times W$



Fully Convolutional network

Ground-truth Normals:

$3 \times H \times W$



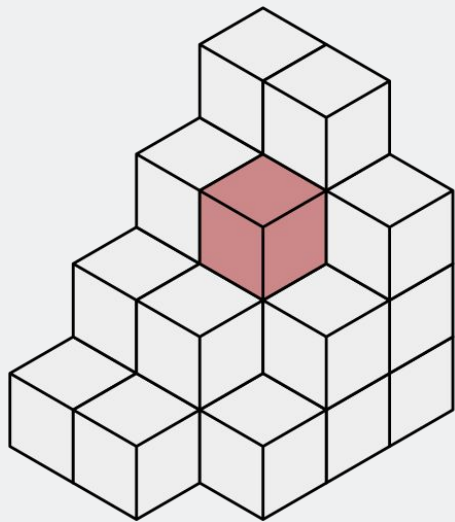
Predicted Normals:
 $3 \times H \times W$

Per-Pixel Loss:
 $(x \cdot y) / (|x| |y|)$

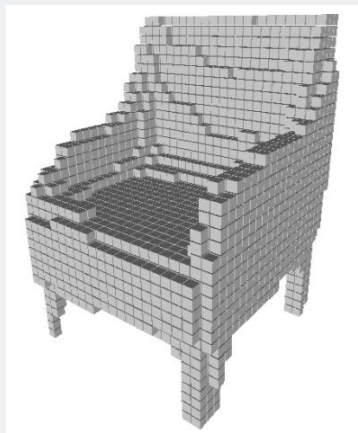
Recall:

$$\begin{aligned} & x \cdot y \\ &= |x| |y| \cos \theta \end{aligned}$$

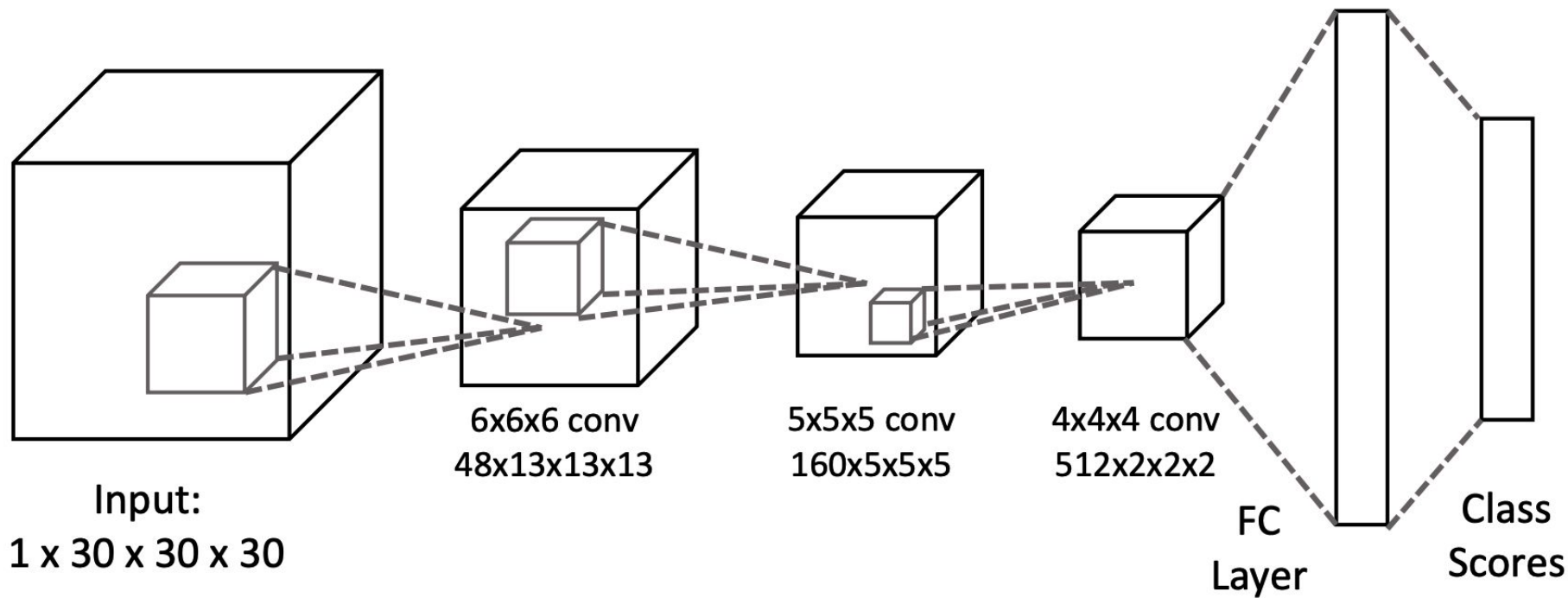
3D Shape Representations: Voxels



- Represent a shape with a $V \times V \times V$ grid of occupancies
- Just like segmentation masks in Mask R-CNN, but in 3D!
- (+) Conceptually simple: just a 3D grid!
- (-) Need high spatial resolution to capture fine structures
- (-) Scaling to high resolutions is nontrivial!



Processing Voxel Inputs: 3D Convolution

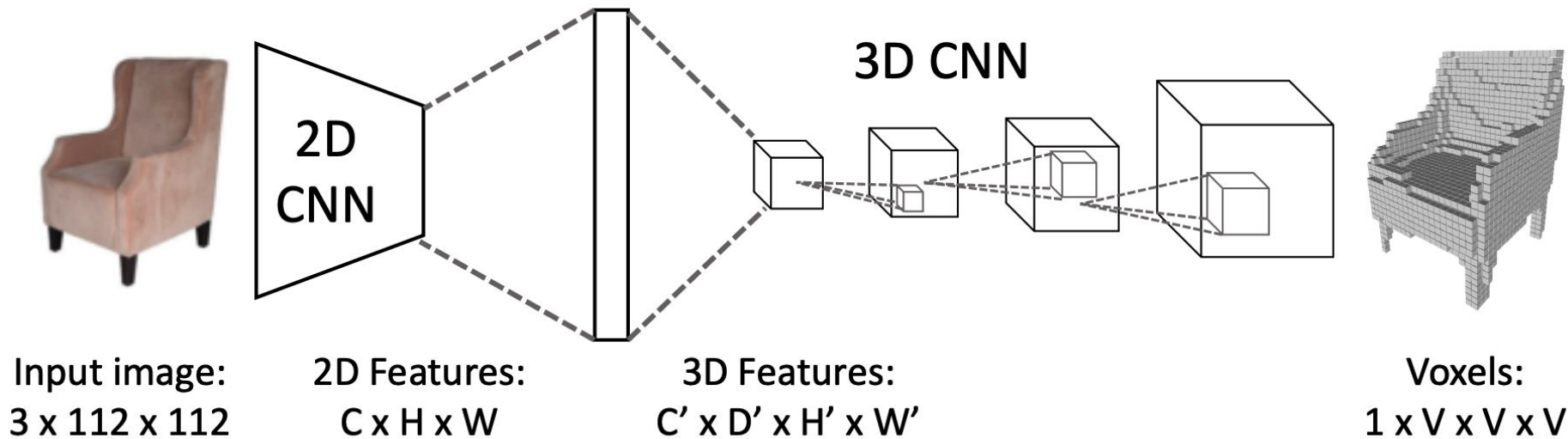


<https://arxiv.org/pdf/1406.5670>

<https://3dshapenets.cs.princeton.edu/>

Train with classification loss

Generating Voxel Shapes: 3D Convolution



<https://arxiv.org/pdf/1604.00449>

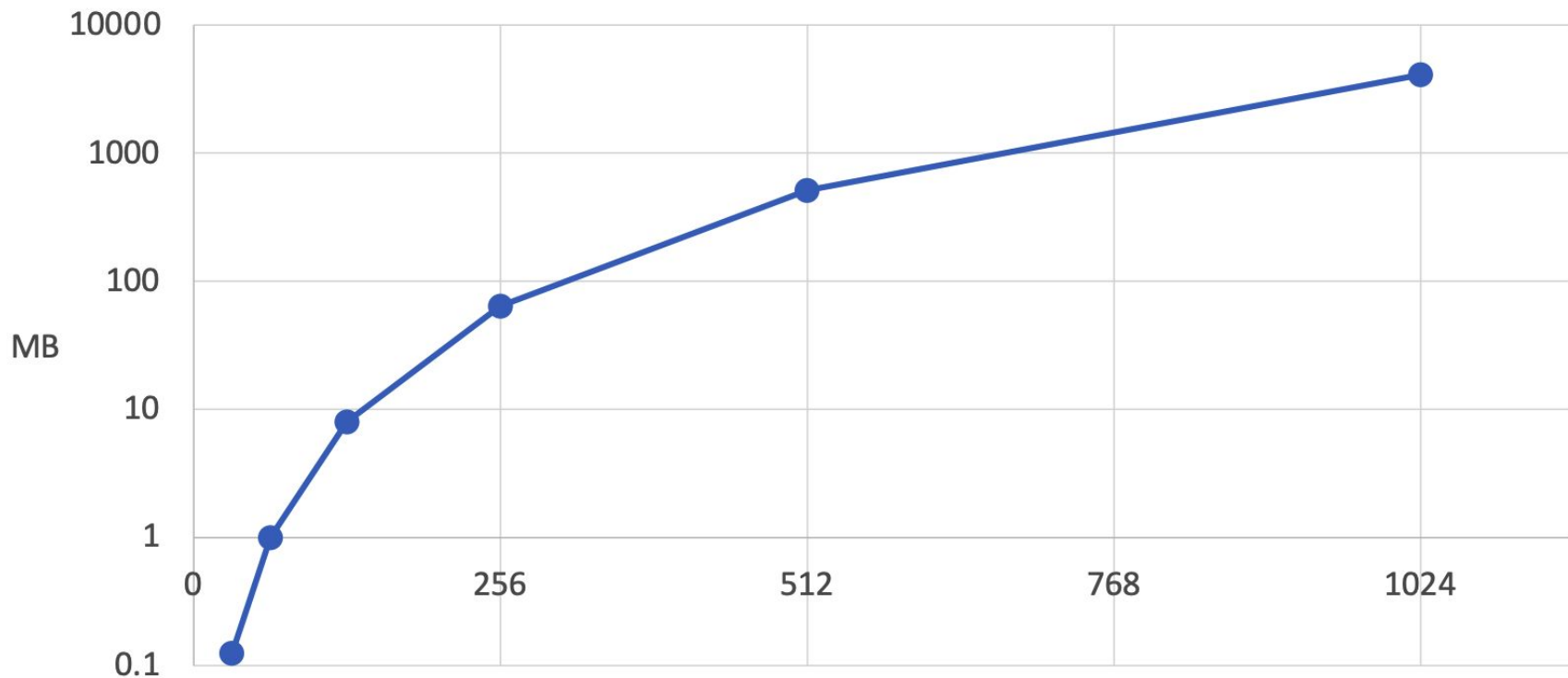
Train with per-voxel cross-entropy loss

Q: voxels with occluded parts?

Voxel: Memory Usage

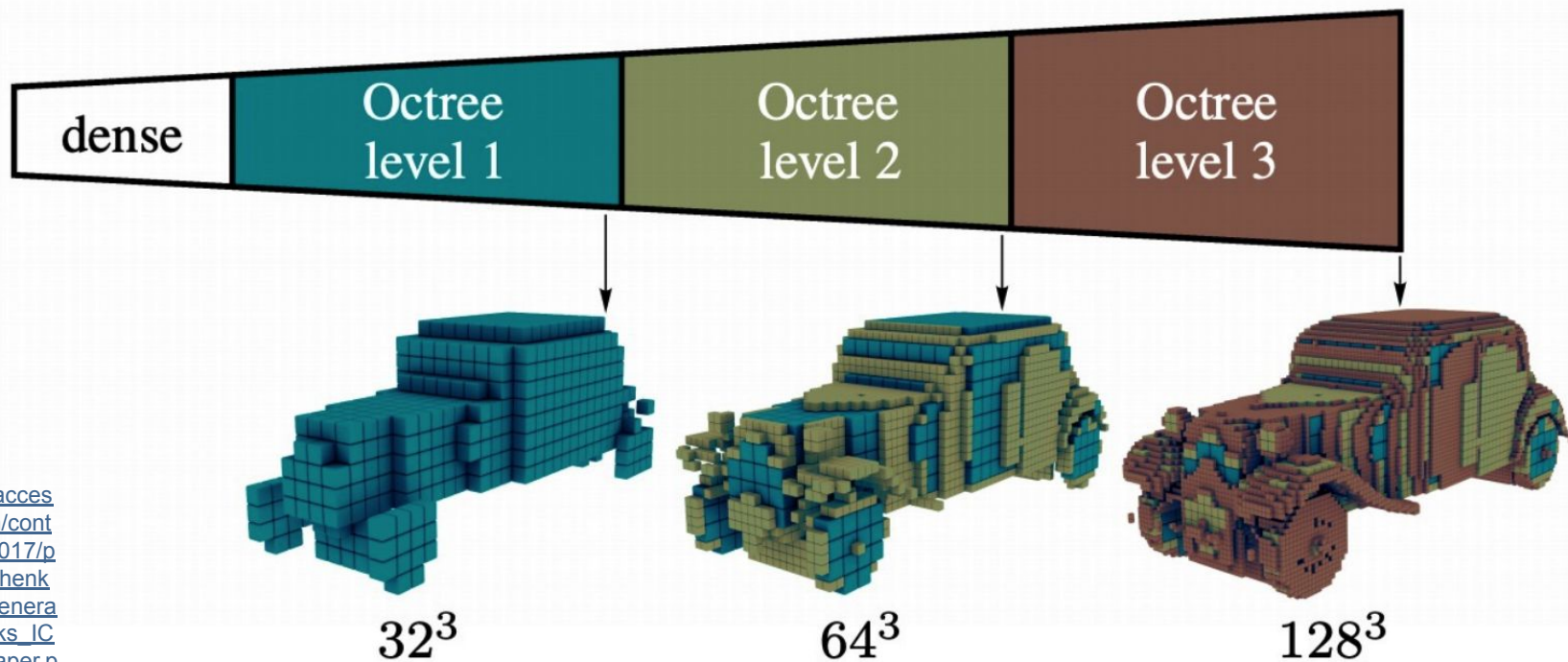
Storing 1024^3 voxel grid takes 4GB of memory!

Voxel memory usage (V x V x V float32 numbers)



Scaling Voxels: Oct-Trees

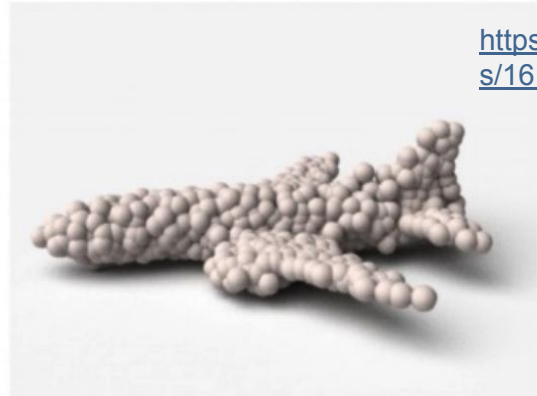
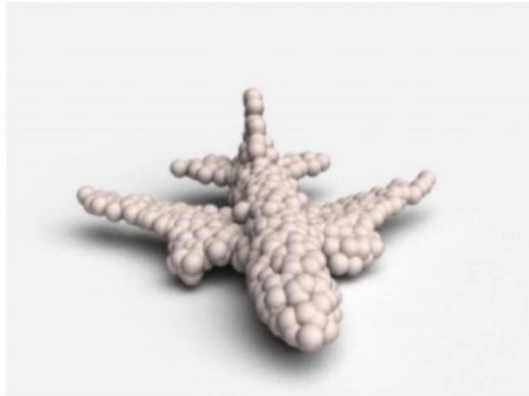
Use voxel grids with heterogenous resolution!



https://openaccess.thecvf.com/content_ICCV_2017/papers/Tatarchenko_Octree_Generating_Networks_ICCV_2017_paper.pdf

3D Shape Representations: Point Cloud

- Represent shape as a set of P points in 3D space
- (+) Can represent fine structures without huge numbers of points
- () Requires new architecture, losses, etc
- (-) Doesn't explicitly represent the surface of the shape: extracting a mesh for rendering or other applications requires post-processing



<https://arxiv.org/abs/1612.00603>

PointNet

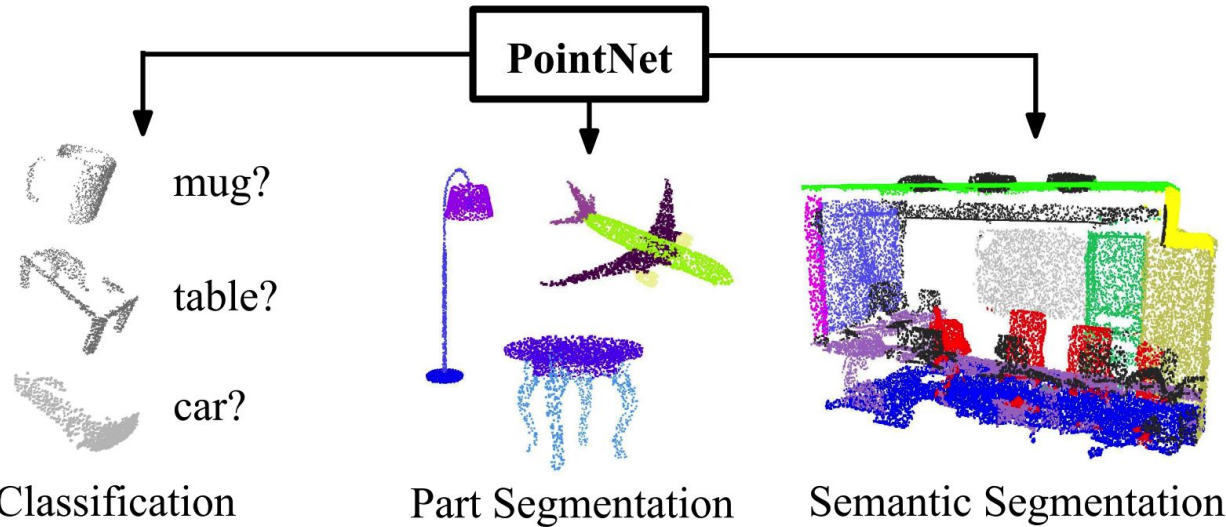
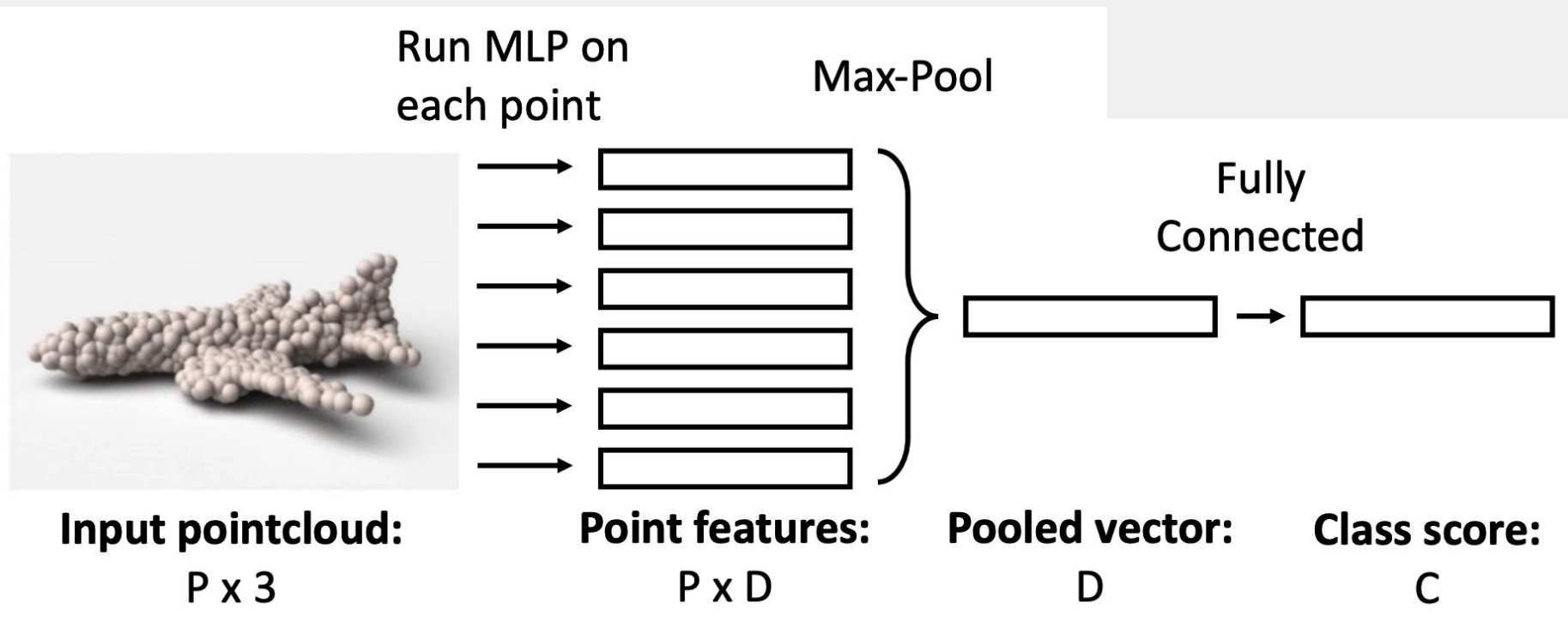


Figure 1. Applications of PointNet. We propose a novel deep net architecture that consumes raw point cloud (set of points) without voxelization or rendering. It is a unified architecture that learns both global and local point features, providing a simple, efficient and effective approach for a number of 3D recognition tasks.

https://openaccess.thecvf.com/content_cvpr_2017/papers/Qi_PointNet_Deep_Learning_CVPR_2017_paper.pdf

PointNet

Q: does order matter?



PointNet and more

PointNet (3D point cloud processing, no voxel or rendering):

https://openaccess.thecvf.com/content_cvpr_2017/papers/Qi_PointNet_Deep_Learning_CVPR_2017_paper.pdf

PointNet++ (adaptively combine features from multiple scales):

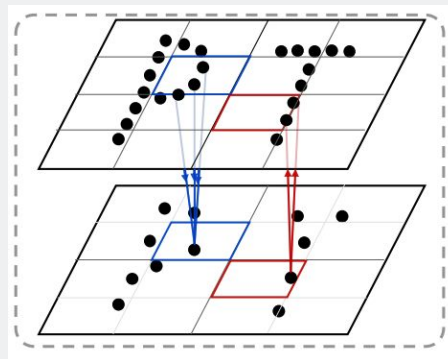
<https://arxiv.org/pdf/1706.02413>

PointNeXt (Improved Training and Scaling Strategies):

https://proceedings.neurips.cc/paper_files/paper/2022/file/9318763d049edf9a1f2779b2a59911d3-Paper-Conference.pdf

Point Transformer (v2) (partition-based group vector attention):

https://proceedings.neurips.cc/paper_files/paper/2022/file/d78ece6613953f46501b958b7bb4582f-Paper-Conference.pdf

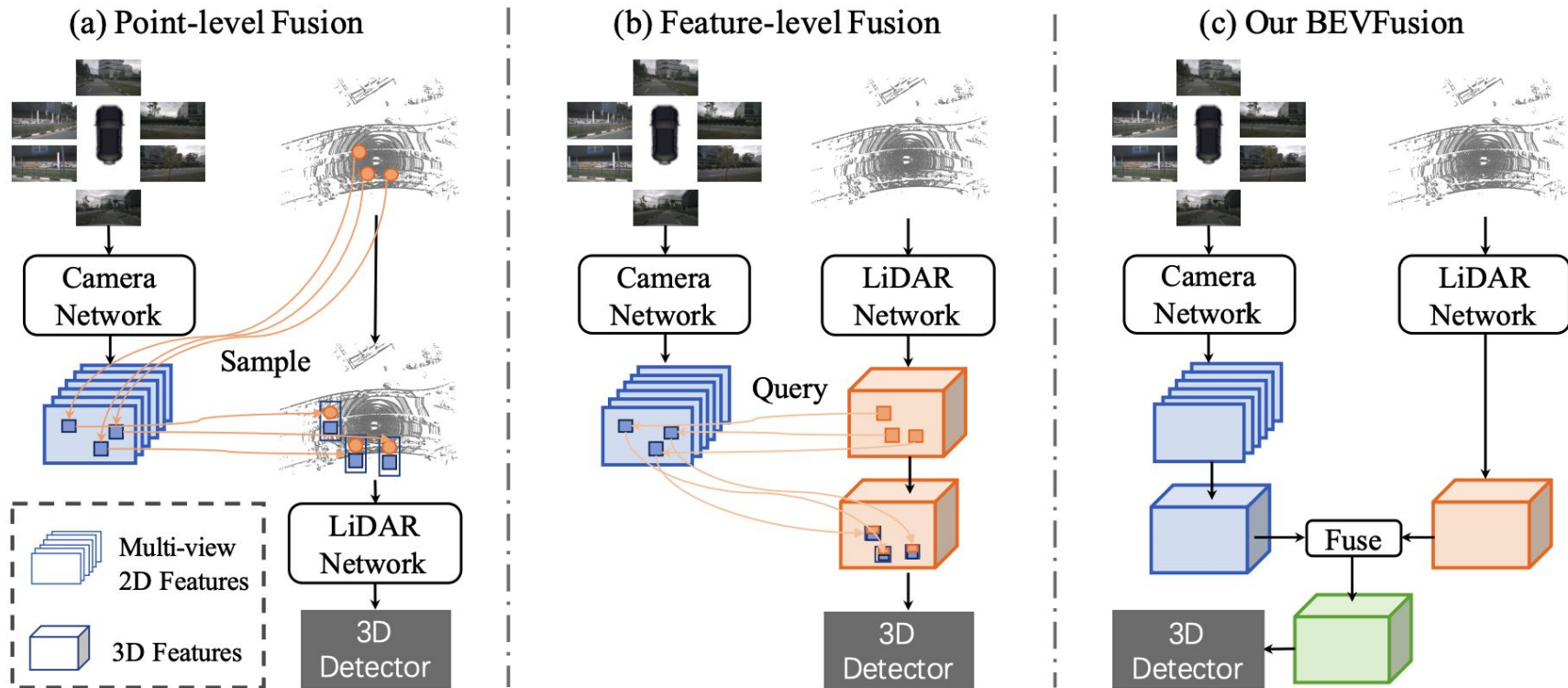


PointNet and more

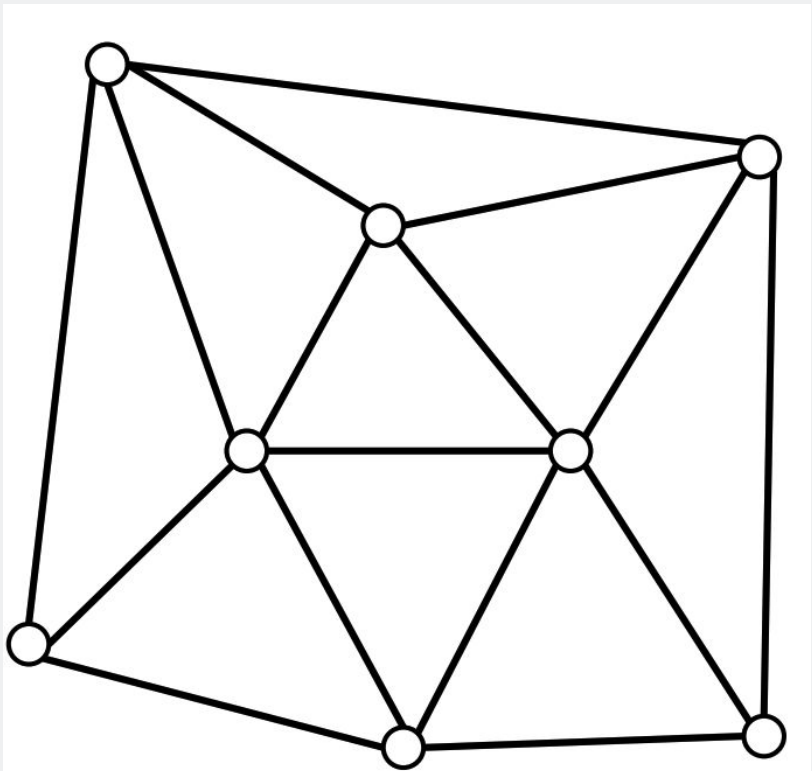
Applications (e.g., LiDAR+Camera Fusion)

BEVFusion

https://proceedings.neurips.cc/paper_files/paper/2022/file/43d2b7fbee8431f7cef0d0afed51c691-Paper-Conference.pdf



3D Shape Representations: Triangle Mesh



Represent a 3D shape as a set of triangles

Vertices: Set of V points in 3D space

Faces: Set of triangles over the vertices

(+) Standard representation for graphics

(+) Explicitly represents 3D shapes

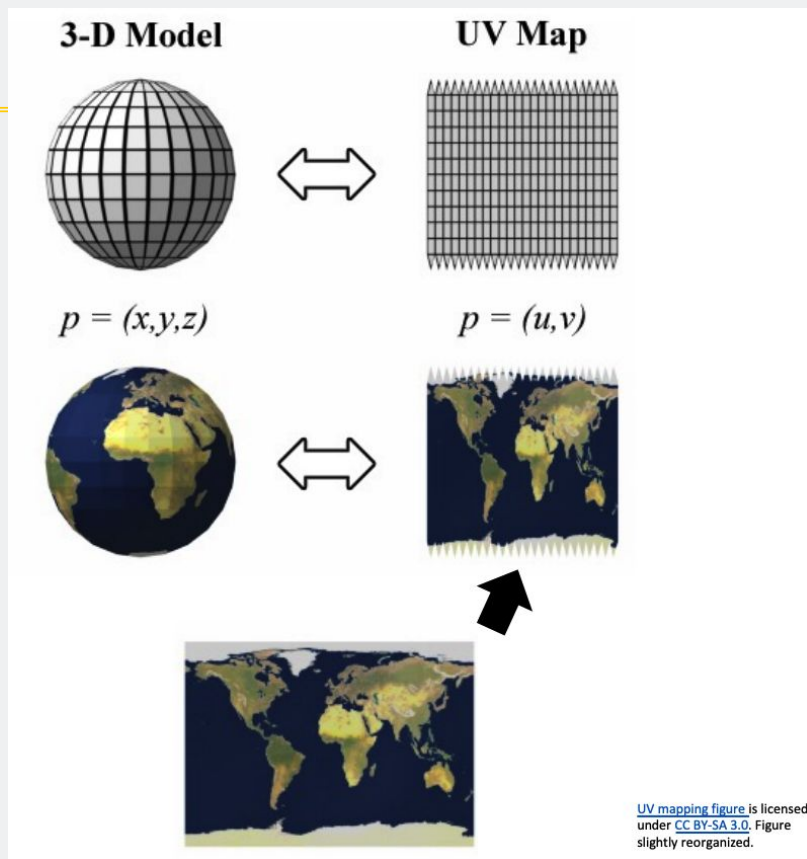
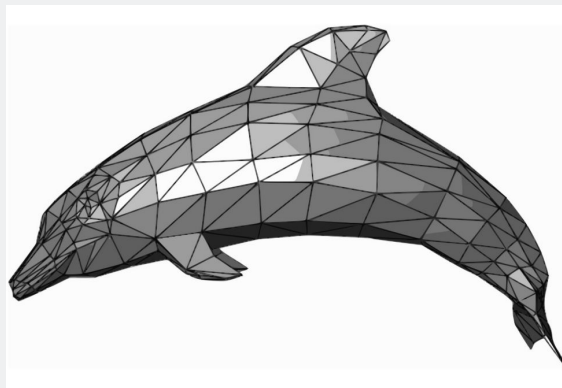
(+) Adaptive: Can represent flat surfaces very efficiently, can allocate more faces to areas with fine detail

(+) Can attach data on verts and interpolate over the whole surface: RGB colors, texture coordinates, normal vectors, etc.

Examples

<https://graphics.stanford.edu/data/3Dscanrep/>

“Stanford bunny”



SMPL

<https://smpl.is.tue.mpg.de/>

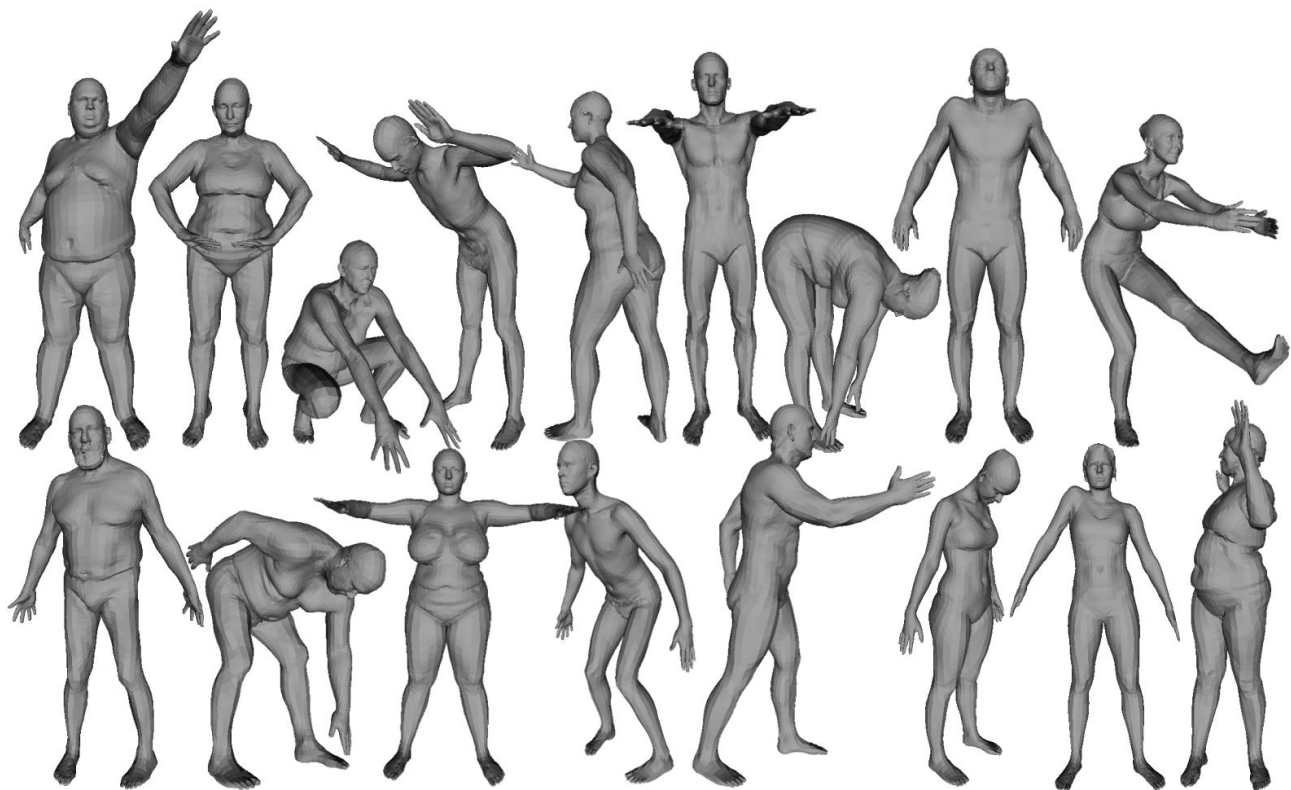
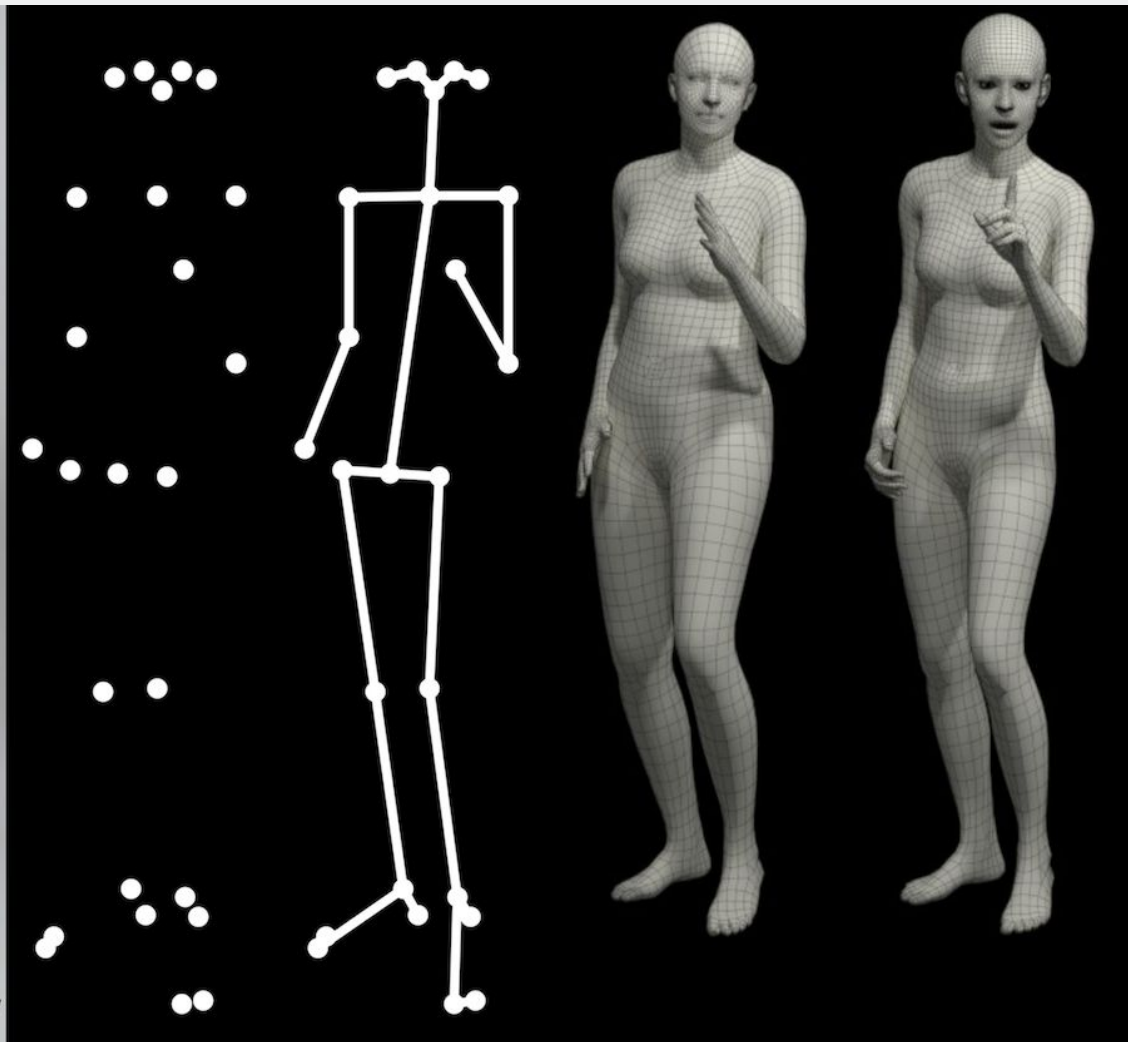


Figure 4: *Sample registrations from the multipose dataset.*

SMPL-X



Original image:
[https://www.gettyimages.com/
search/stack/546047069#](https://www.gettyimages.com/search/stack/546047069#)

<https://smpl-x.is.tue.mpg.de/>

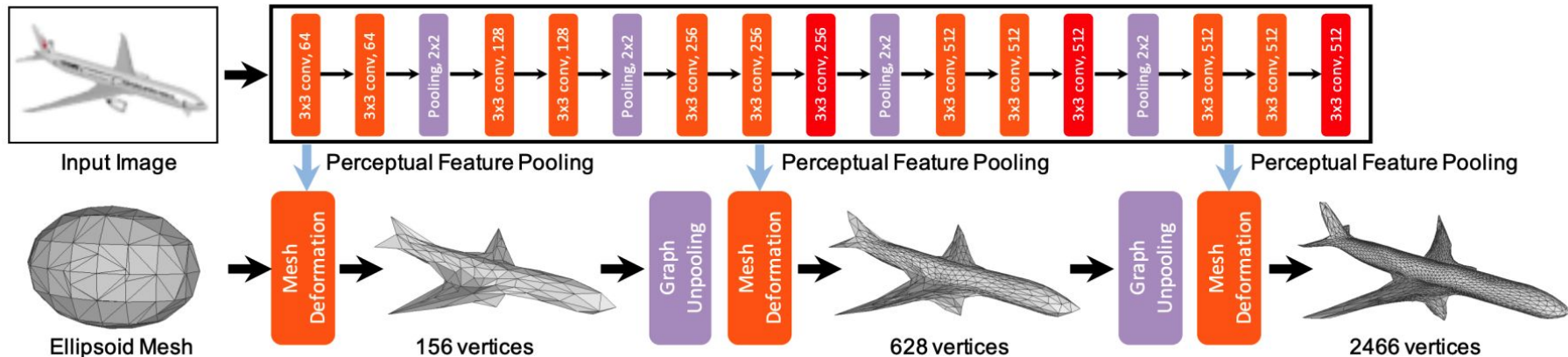
Predicting Meshes: Pixel2Mesh

Input: Single RGB
Image of an object

Key ideas:

- Iterative Refinement
- Graph Convolution
- Vertex Aligned-Features
- Chamfer Loss Function

Output: Triangle
mesh for the object



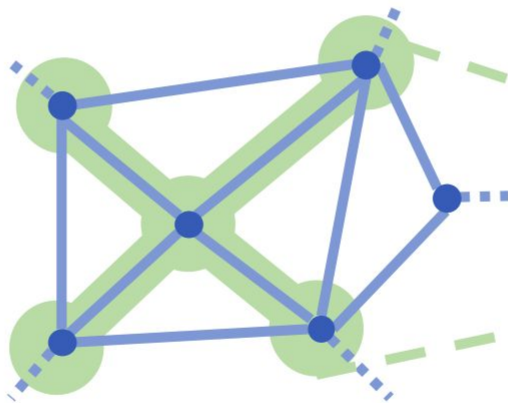
Graph Convolution

$$f'_i = W_0 f_i + \sum_{j \in N(i)} W_1 f_j$$

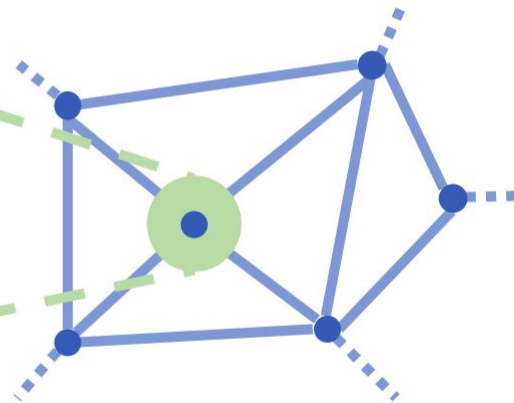
Vertex v_i has feature f_i

New feature f'_i for vertex v_i depends on feature of neighboring vertices $N(i)$

Use same weights W_0 and W_1 to compute all outputs



Input: Graph with a feature vector at each vertex



Output: New feature vector for each vertex

3D Shape Representations: Implicit Functions

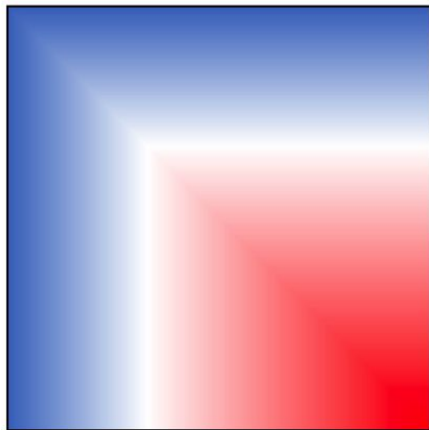
Learn a function to classify arbitrary 3D points as inside / outside the shape

$$o : \mathbb{R}^3 \rightarrow \{0, 1\}$$

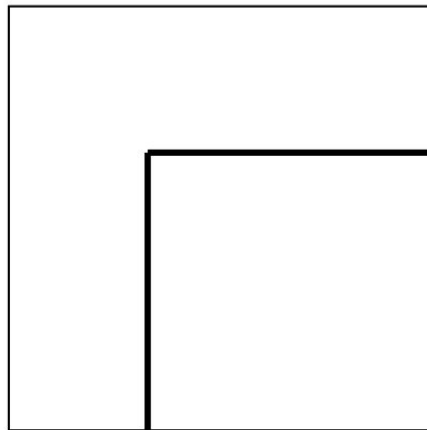
The surface of the 3D object is the level set

$$\{x : o(x) = \frac{1}{2}\}$$

Binary
classification
problem



Implicit function



Explicit Shape

- Occupancy
- SDF (signed distance function)

Neural Radiance Field (NeRF) For View Synthesis

<https://arxiv.org/pdf/2003.08934>

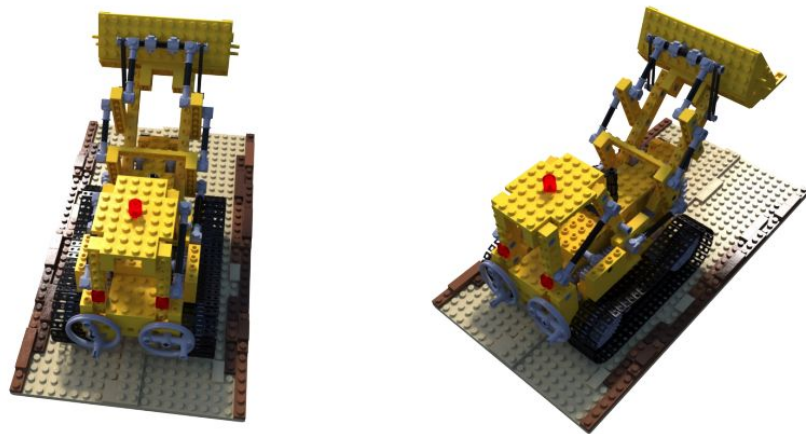
View Synthesis

<https://www.matthewtancik.com/nerf>

Input: Many images of the same scene
(with known camera parameters)

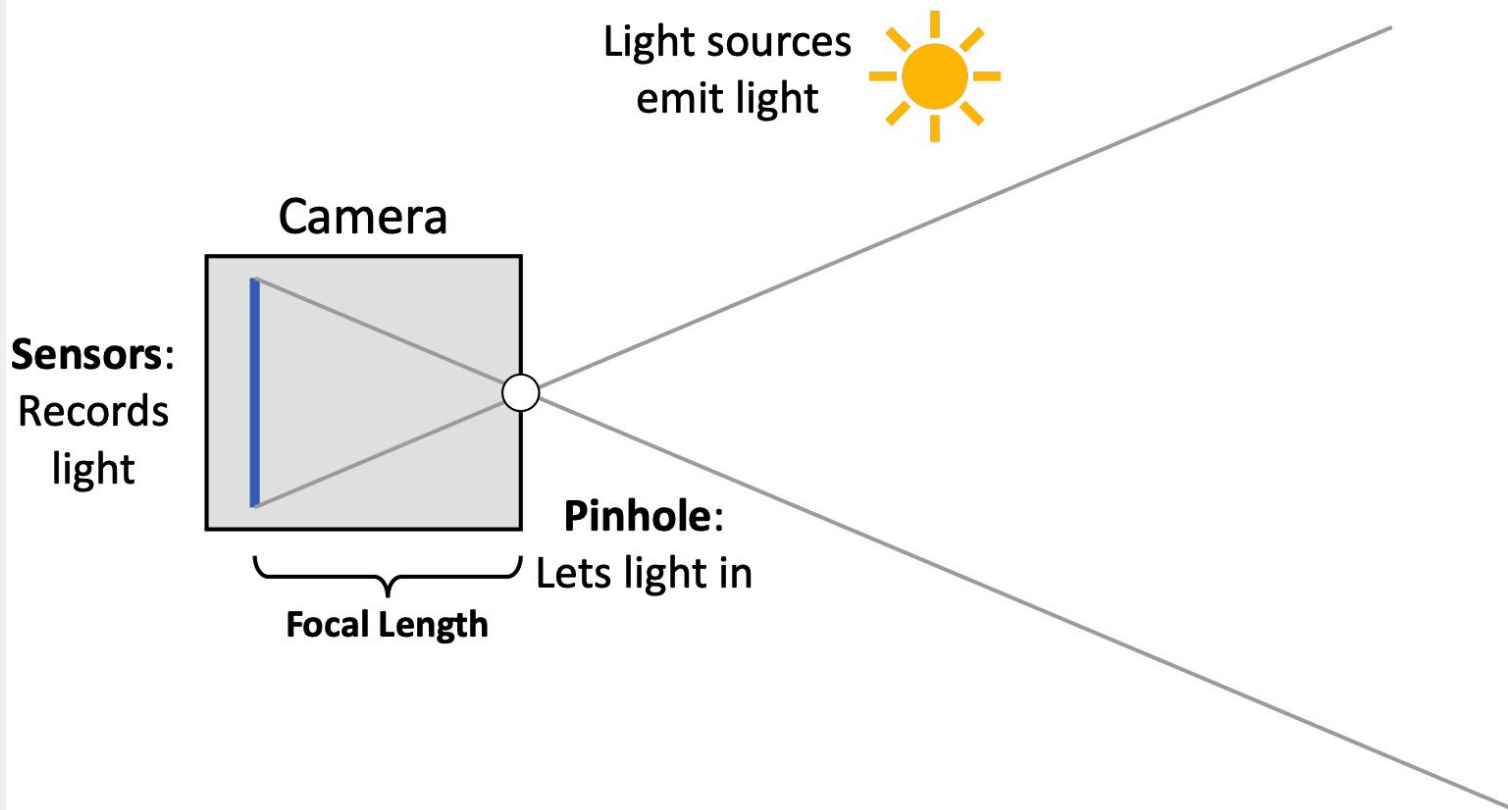


Output: Images showing the scene from novel viewpoints

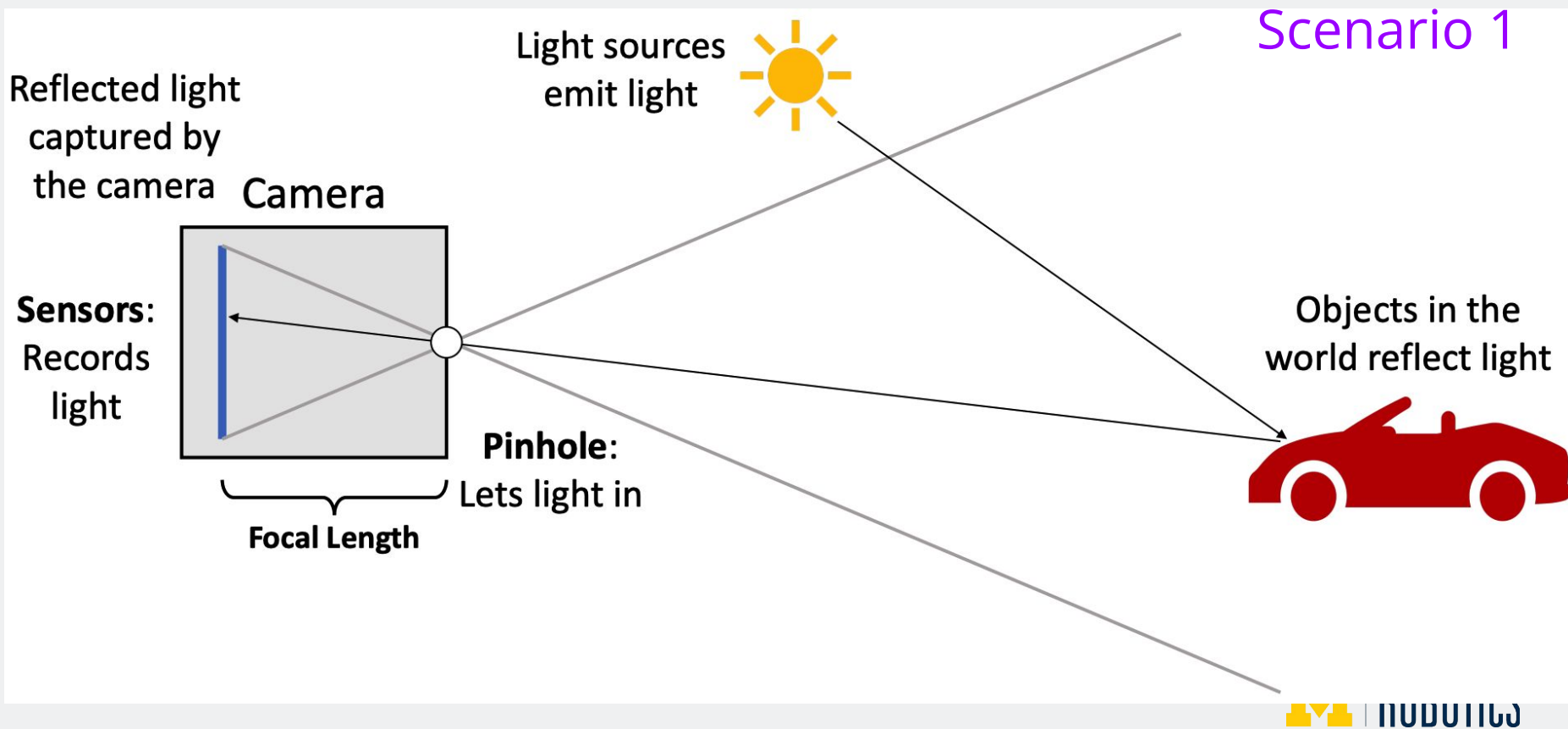


Scene rendering

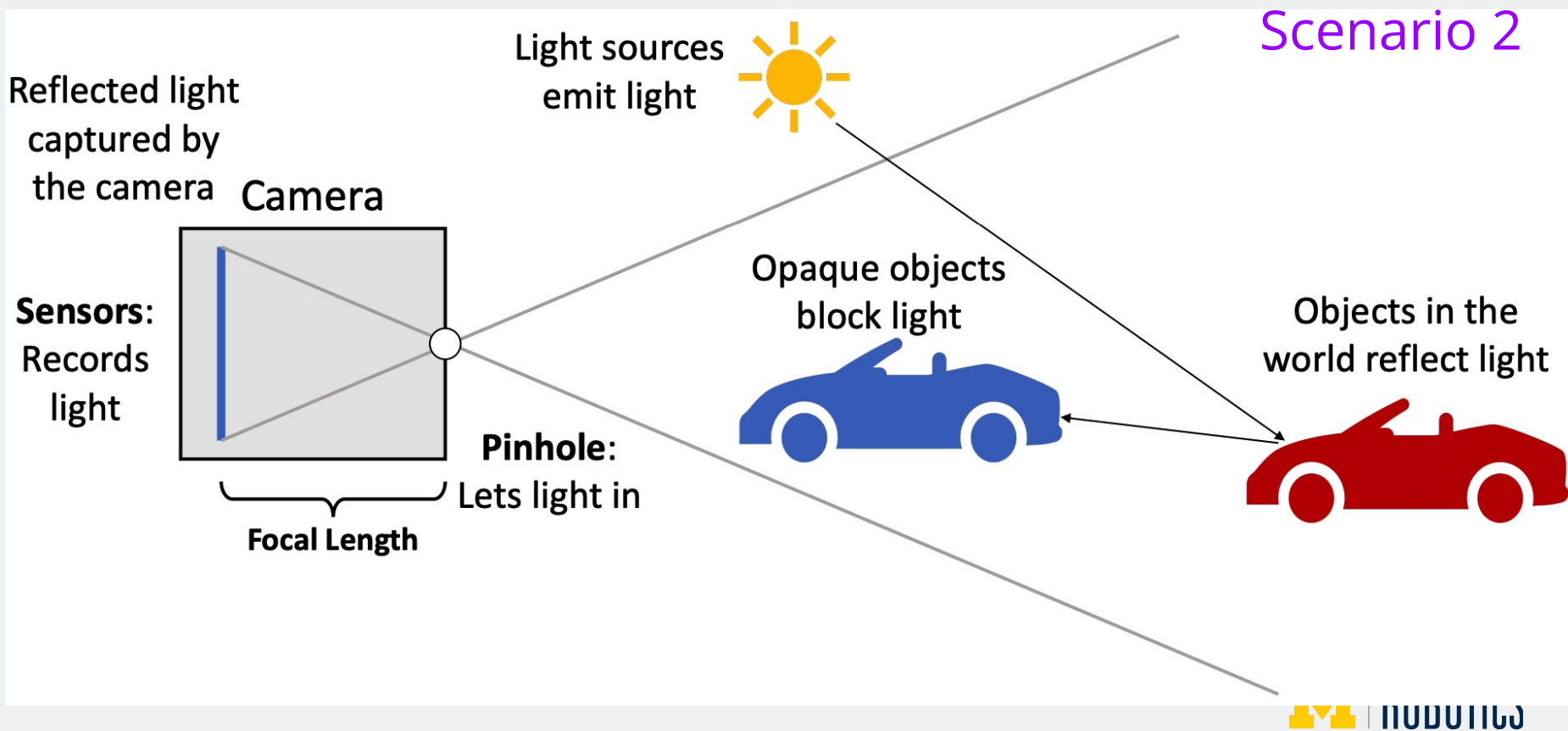
Stepping Back: Pinhole Camera Model



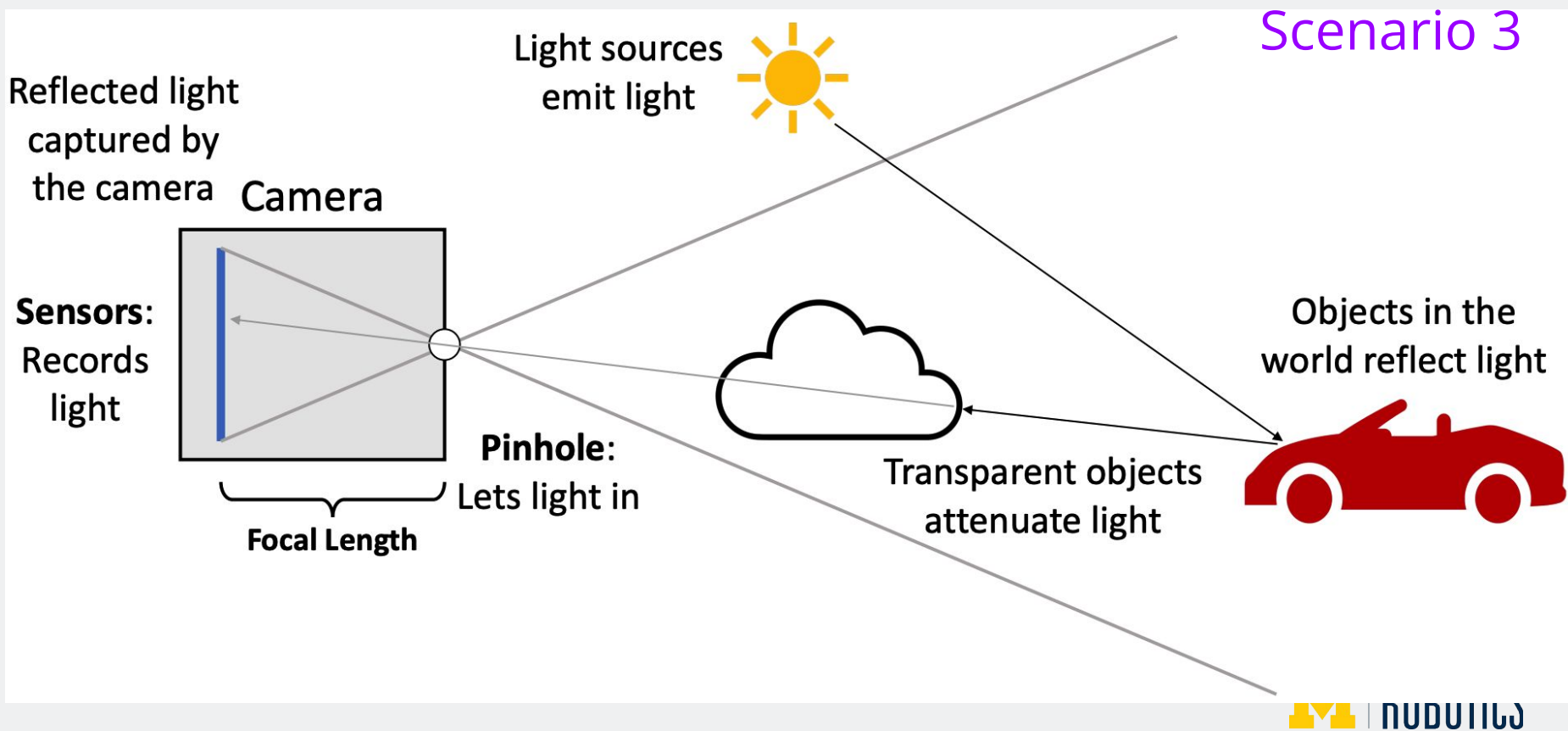
Stepping Back: Pinhole Camera Model



Stepping Back: Pinhole Camera Model



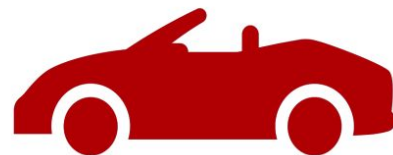
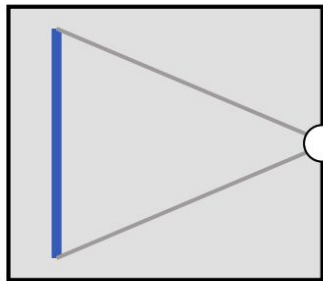
Stepping Back: Pinhole Camera Model



Volume Rendering

Abstract away light sources, objects.
For each point in space, need to know:

- (1) How much light does it emit?
- (2) How opaque is it? $\sigma \in [0,1]$

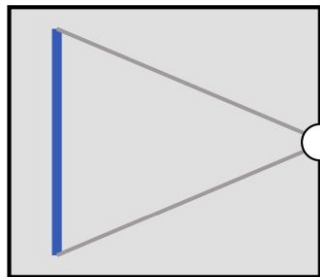


Stepping Back: Pinhole Camera Model

Abstract away light sources, objects.

For each point in space, need to know:

- (1) How much light does it emit?
- (2) How opaque is it? $\sigma \in [0,1]$

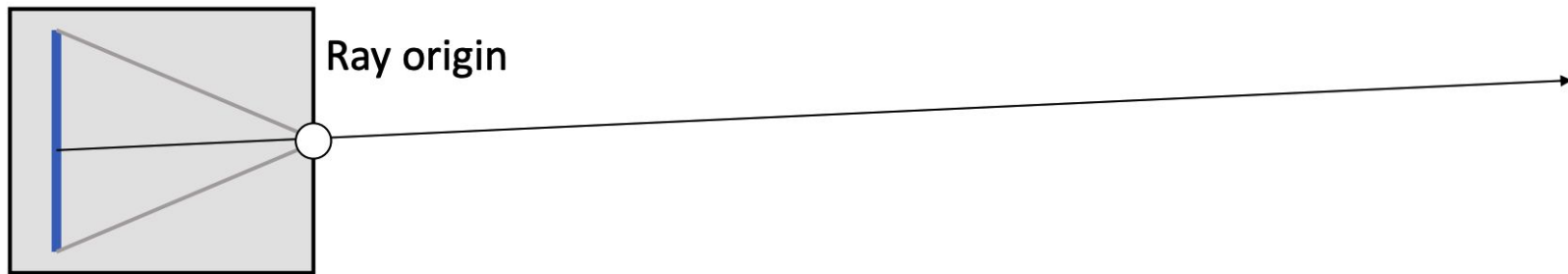


Point in empty space:
(1) Emits no light (black)
(2) Completely transparent $\sigma = 0$

Point on car:
(1) Emits red light in hemisphere
(2) Complete opaque $\sigma = 1$



Volume Rendering



Parameterize each ray as origin plus

direction: $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$

Volume Density is $\sigma(\mathbf{p}) \in [0,1]$

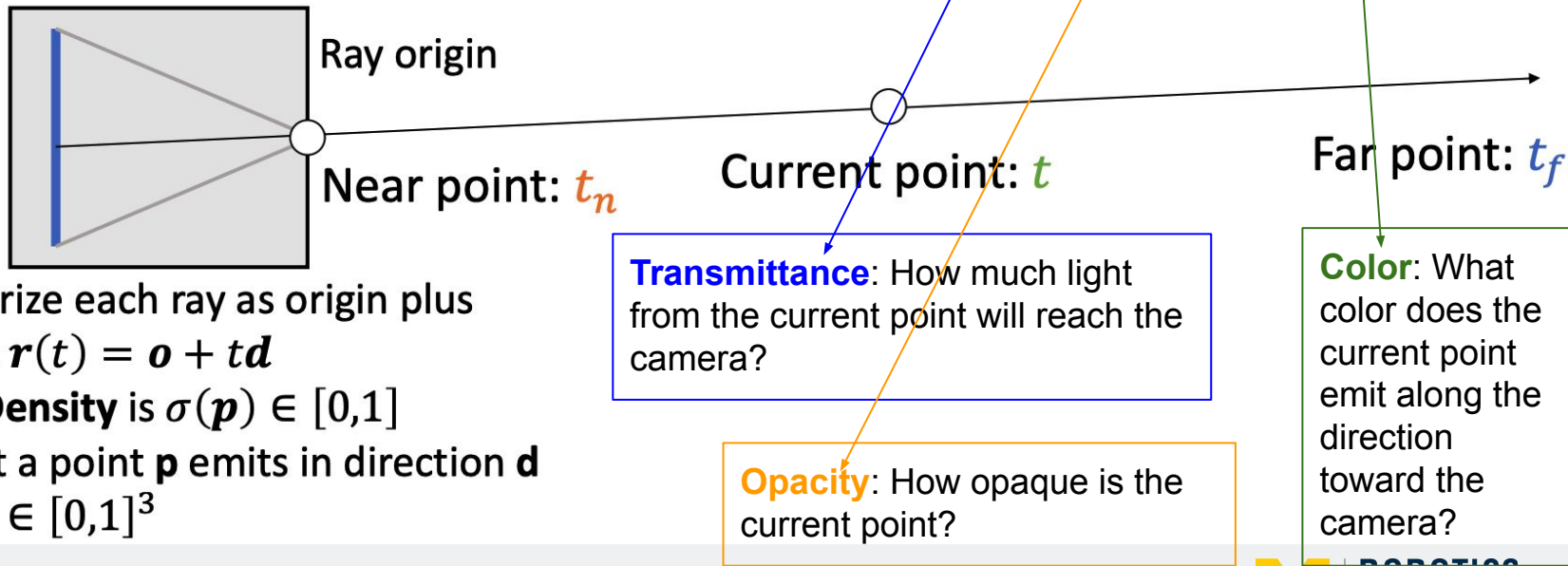
Color that a point $\mathbf{p}$ emits in direction $\mathbf{d}$

is $c(\mathbf{p}, \mathbf{d}) \in [0,1]^3$

Volume Rendering

Color observed by the camera given by **volume rendering equation**:

$$C(\mathbf{r}) = \int_{t_n}^{t_f} \underbrace{T(t)}_{\text{Transmittance}} \underbrace{\sigma(\mathbf{r}(t))}_{\text{Opacity}} \underbrace{c(\mathbf{r}(t), \mathbf{d})}_{\text{Color}} dt$$



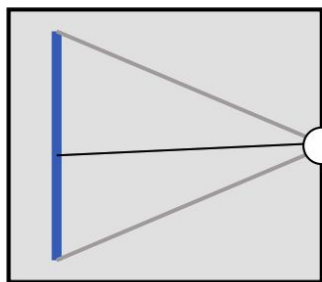
Parameterize each ray as origin plus direction: $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$

Volume Density is $\sigma(\mathbf{p}) \in [0,1]$

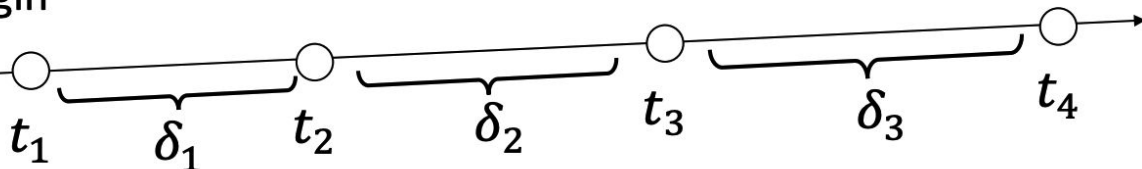
Color that a point $\mathbf{p}$ emits in direction $\mathbf{d}$ is $c(\mathbf{p}, \mathbf{d}) \in [0,1]^3$

Transmittance

Compute transmittance by
accumulating volume
density up to current point



Ray origin



Approximate integrals with a set of samples:

$$C(\mathbf{r}) \approx \sum_{i=1}^N T_i (1 - \exp(-\sigma_i \delta_i)) \mathbf{c}_i$$

$$T_i = \exp\left(-\sum_{j=1}^{i-1} \sigma_j \delta_j\right)$$

Mildenhall et al, "Representing
Scenes as Neural Radiance Fields
for View Synthesis", ECCV 2020

Parameterize each ray as origin plus
direction: $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$

Volume Density is $\sigma(\mathbf{p}) \in [0,1]$

Color that a point $\mathbf{p}$ emits in direction $\mathbf{d}$
is $c(\mathbf{p}, \mathbf{d}) \in [0,1]^3$

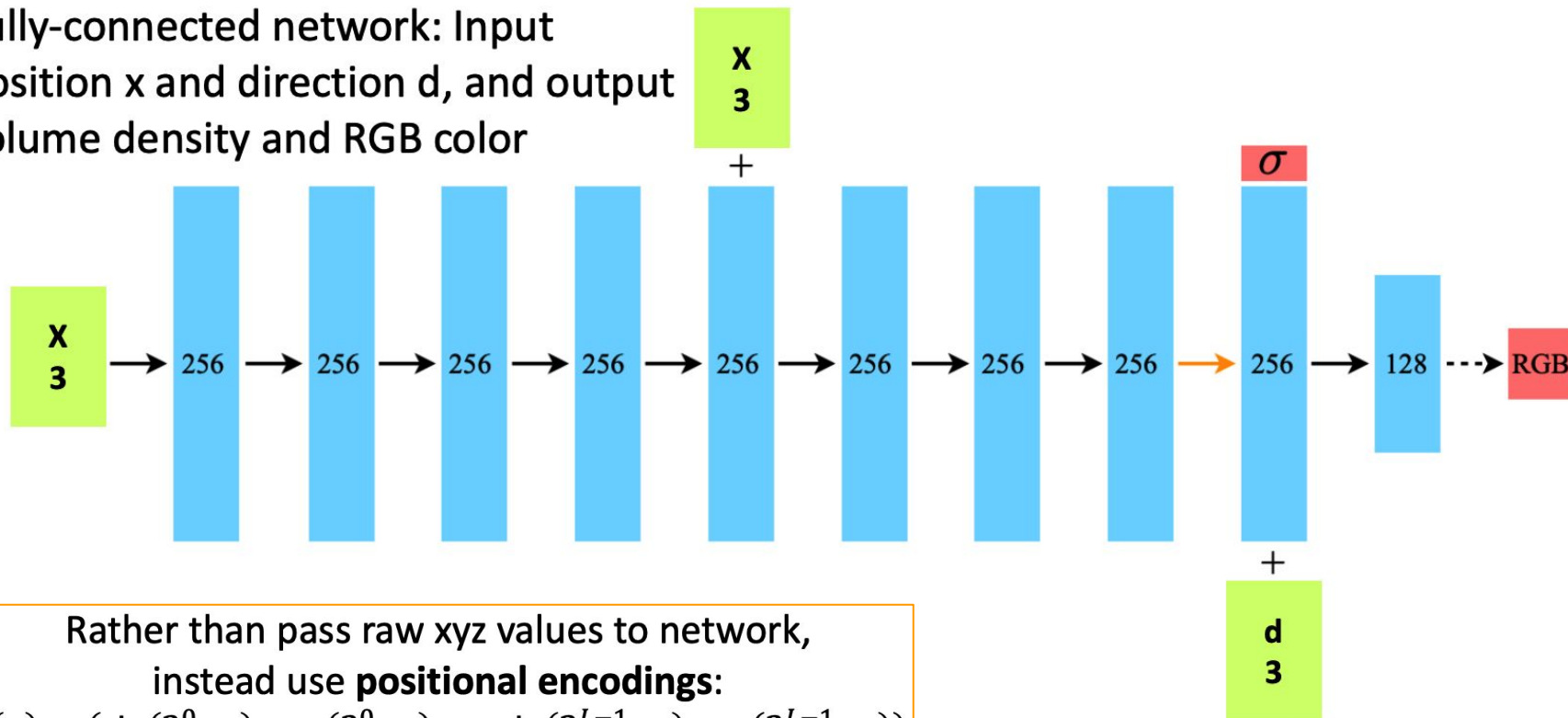
NeRF

Train a neural network to input position $\mathbf{p}$
and direction $\mathbf{d}$, output $\sigma(\mathbf{p})$ and $c(\mathbf{p}, \mathbf{d})$

Training loss: Estimated pixel colors $\mathcal{C}(\mathbf{r})$
should match actual pixel colors from images

NeRF: Network Architecture

Fully-connected network: Input position x and direction d , and output volume density and RGB color



Rather than pass raw xyz values to network,
instead use **positional encodings**:
 $\gamma(p) = (\sin(2^0\pi p), \cos(2^0\pi p), \dots, \sin(2^{L-1}\pi p), \cos(2^{L-1}\pi p))$

NeRF: Network Architecture

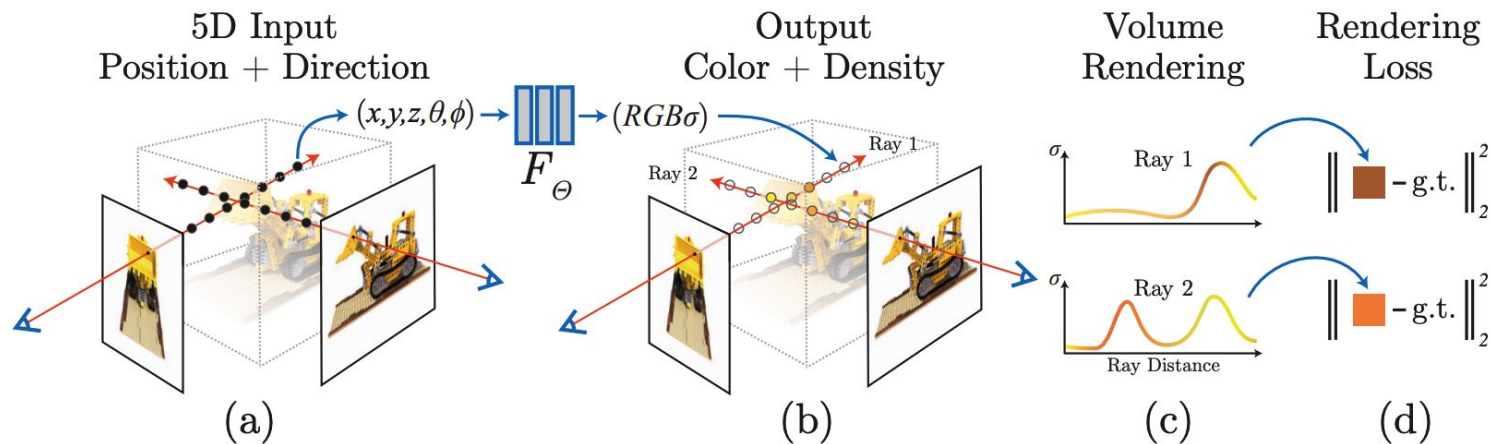


Fig. 2: An overview of our neural radiance field scene representation and differentiable rendering procedure. We synthesize images by sampling 5D coordinates (location and viewing direction) along camera rays (a), feeding those locations into an MLP to produce a color and volume density (b), and using volume rendering techniques to composite these values into an image (c). This rendering function is differentiable, so we can optimize our scene representation by minimizing the residual between synthesized and ground truth observed images (d).

NeRF



NeRF (2020)

Main Problem: Very slow!

Training: 1-2 days on a V100 GPU, for just a single scene!

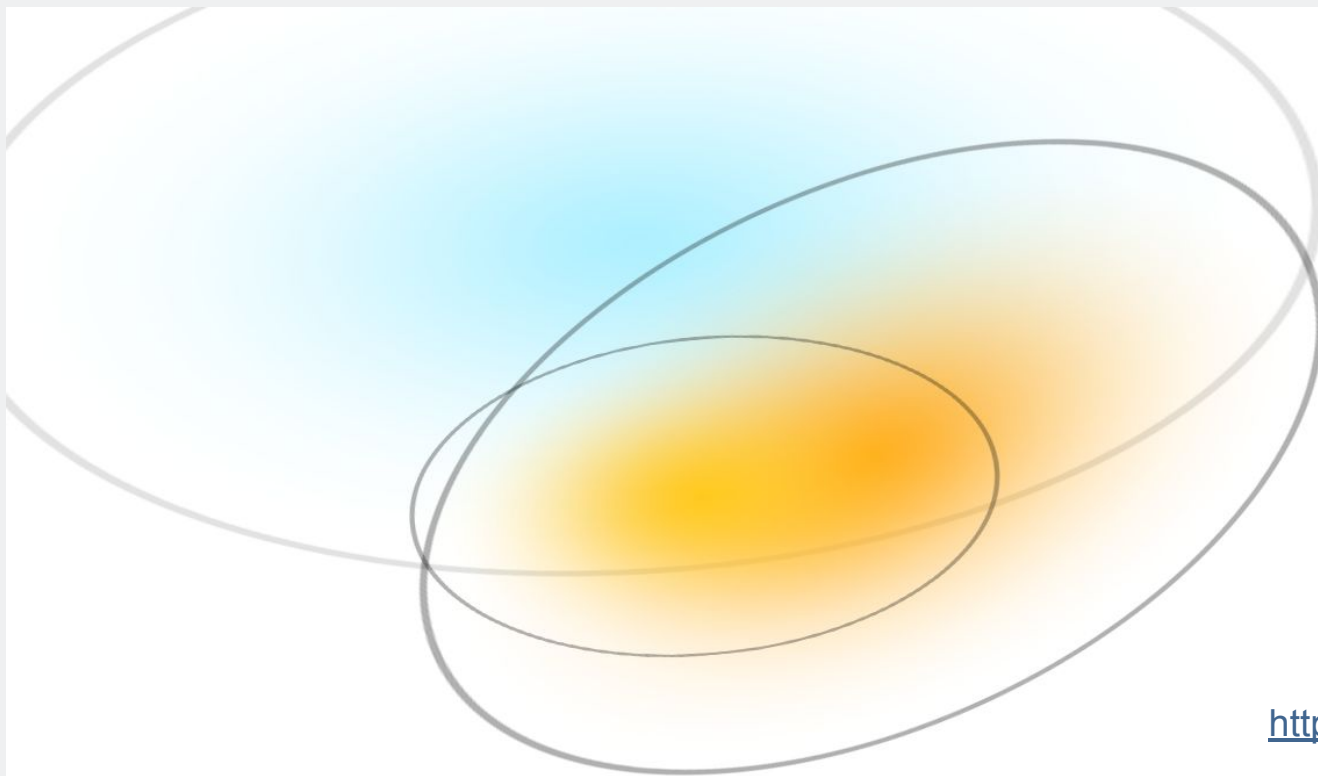
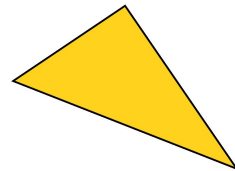
Inference: Sampling an image from a trained model:
(256 x 256 pixels) x (224 samples per pixel)
= 14.6M forward passes through MLP

Tons of follow-up work!

Cited by 11521

Gaussian Splatting (2023)

Recall: Triangle Meshes



<https://arxiv.org/pdf/2308.04079>

Gaussian Splatting

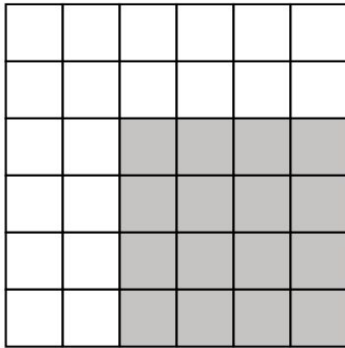


(More on this)

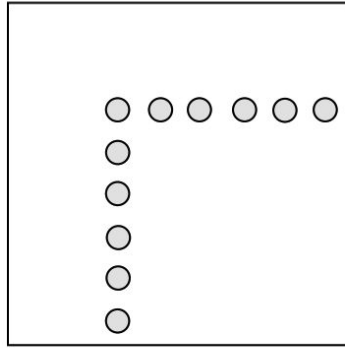
Summary



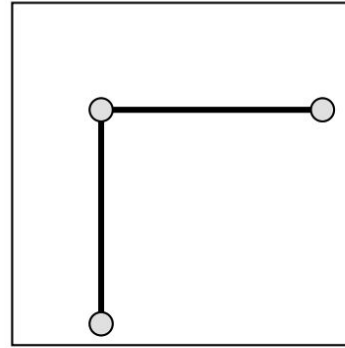
Depth
Map



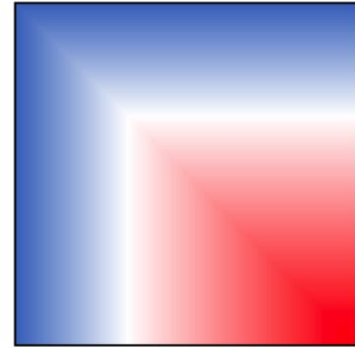
Voxel
Grid



Pointcloud



Mesh



Implicit
Surface

Reminder:

- **Final Project** “lightning talk” April 1, 2025 (tomorrow during discussion)
- **Canvas Quiz**

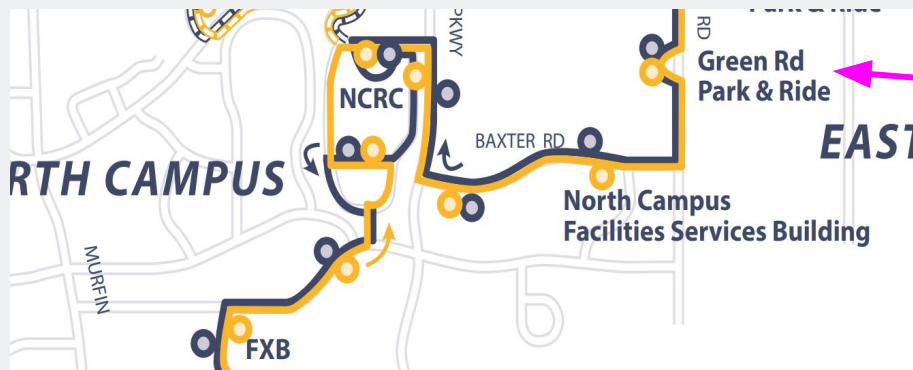
MCity Data Collection

Tomorrow (April 1st), 8am EST

Reach out to Cale Colony (GSI) ccolony@umich.edu

Dress warmly (26-44F)

<https://piazza.com/class/m4pgejar4ua2qf/post/228>



MCity