



### Lecture 12 **Deep Learning Software University of Michigan I Department of Robotics**







### 1. One time setup:

- Activation functions, data preprocessing, weight initialization, regularization
- 2. Training dynamics:
- **3.** After training:



### Overview

### Learning rate schedules; hyperparameter optimization

### • Model ensembles, transfer learning, large-batch training





**1.** Train multiple independent models 2. At test time average their results: (Take average of predicted probability distributions, then choose argmax)

Enjoy 2% extra performance



### Model Ensembles



## Model Ensembles: Tips and Tricks

### Instead of training independent models, use multiple snapshots of a single model during training!



Loshchilov and Hutter, "SGDR: Stochastic gradient descent with restarts", arXiv 2016

Huang et al, "Snapshot ensembles: train 1, get M for free", ICLR 2017 Figures copyright Yixuan Li and Geoff Pleiss, 2017. Reproduced with permission.





Cyclic learning rate schedules can make this work even better!





## Model Ensembles: Tips and Tricks

Instead of using actual parameter vector, keep a moving average of the parameter vector and use that at test time (Polyak averaging)

while True: data batch = dataset.sample data batch() loss = network.forward(data batch) dx = network.backward()x += - learning rate \* dx

Polyak and Juditsky, "Acceleration of stochastic approximation by averaging", SIAM Journal on Control and Optimization, 1992.

Karras et al, "Progressive Growing of GANs for Improved Quality, Stability, and Variation", ICLR 2018 Brock et al, "Large Scale GAN Training for High Fidelity Natural Image Synthesis", ICLR 201

```
x test = 0.995*x test + 0.005*x # use for test set
```



### "You need a lot of data if you want to train / use CNNs"

### What if data is limited?



### Transfer Learning



## Transfer Learning with CNNs

### 1. Train on ImageNet





DEEPRESSION et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014



## Transfer Learning with CNNs

### 1. Train on ImageNet





DEEP Rophs bonance et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014





## **Transfer Learning with CNNs**

### 1. Train on ImageNet





DEEPROFICE et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014





### 1. Train on ImageNet



### 2. Use CNN as a feature extractor



DEEP Recognition", CVPR Workshops 2014

Prior State of the art CNN + SVM CNN + Augmentation + SVM



## **Transfer Learning with CNNs**

### 1. Train on ImageNet



### 2. Use CNN as a feature extractor



### Image Retrieval: Nearest-Neighbor

DEEPREASE al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014



### 1. Train on ImageNet

FC-1000
FC-4096
FC-4096
MaxPool
Conv-512
Conv-512
MaxPool
Conv-512
Conv-512
MaxPool
Conv-256
Conv-256
MaxPool
Conv-128
Conv-128
MaxPool
Conv-64
Conv-64
Image





## 3. Bigger dataset: **Fine-Tuning**



Continue training CNN for new task!



### 1. Train on ImageNet

FC-1000
FC-4096
FC-4096
MaxPool
Conv-512
Conv-512
MaxPool
Conv-512
Conv-512
MaxPool
Conv-256
Conv-256
MaxPool
Conv-128
Conv-128
MaxPool
Conv-64
Conv-64
Image





## 3. Bigger dataset: **Fine-Tuning**



Continue training CNN for new task!

### Some tricks:

- Train with feature extraction first before fine-tuning
- Lower the learning rate: use ~1/10 of LR used in original training
- Sometimes freeze lower layers to save computation
- Train with BatchNorm in "test" mode





### 1. Train on ImageNet

FC-1000
FC-4096
FC-4096
MaxPool
Conv-512
Conv-512
MaxPool
Conv-512
Conv-512
MaxPool
Conv-256
Conv-256
MaxPool
Conv-128
Conv-128
MaxPool
Conv-64
Conv-64
Image





## 3. Bigger dataset: **Fine-Tuning**



Continue training CNN for new task!

### **Object Detection**





## Transfer Learning: Fine Tuning

### 1. Train on ImageNet





Continue training entire model for new task

## Compared with feature extraction, fine-tuning:

- Requires more data
- Is computationally expensive
- Can give higher accuracies



### Transfer Learning with CNNs: Architecture Matters!







	Dataset similar to ImageNet	Dataset very differ from ImageNet
little data (10s to 100s)	Use Linear Classifier on top layer	You're in trouble. Try linear classifier f different stages
a lot of data (100s to 1000s)	Finetune a few layers	Finetune a large number of layers





### Transfer Learning is pervasive! Its the norm, not the exception



Girshick, "Fast R-CNN", ICCV 2015 Figure copyright Ross Girshick, 2015. Reproduced with permission.



Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015



### Transfer Learning is pervasive! Its the norm, not the exception



Girshick, "Fast R-CNN", ICCV 2015 Figure copyright Ross Girshick, 2015. Reproduced with permission.



with word2vec

Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments" for Generating Image Descriptions", CVPR 2015

### Transfer Learning is pervasive! Its the norm, not the exception



- 1. Train CNN on ImageNet
- 2. Fine-Tune (1) for object detection on Visual Genome
- 3. Train BERT language model on lots of text
- 4. Combine (2) and (3), train for joint image / language modeling
- 5. Fine-tune (5) for image captioning, visual question answering, etc.

Zhou et al, "Unified Vision-Language Pre-Training for Image Captioning and VQA", arXiv 2019



### Transfer Learning is pervasive! Some very recent results have questioned it

### COCO object detection



Training from scratch can work as well as pertaining on ImageNet!

... if you train for 3x as long

He et al, "Rethinking ImageNet Pre-Training", ICCV 2019





### COCO object detection





Transfer Learning is pervasive! Some very recent results have questioned it

> Pretraining + Finetuning beats training from scratch when dataset size is very small

> Collecting more data is more effective than pretraining

> > He et al, "Rethinking ImageNet Pre-Training", ICCV 2019





### Transfer Learning is pervasive! Some very recent results have questioned it

### COCO object detection





My current view on transfer learning:

- Pretrain + finetune makes your training faster, so practically very useful
- Training from scratch works well once you have enough data
- Lots of work left to be done







### 1. One time setup: Activation functions, data preprocessing, weight initialization, regularization 2. Training dynamics: Learning rate schedules; hyperparameter optimization **3.** After training: • Model ensembles, transfer learning



### Summary





## A zoo of frameworks!





(Facebook)

(Facebook)

TensorFlow

Darknet (Redmon)

**MXNet** 

### (Amazon)

Developed by U Washington, CMU, MIT, Hong Kong U, etc. but main framework of choice at AWS

PaddlePaddle

(Baidu)

Chainer

CNTK

(Microsoft)

JAX

(Google)







## A zoo of frameworks!



(Facebook)

TensorFlow

We'll focus on these

Darknet (Redmon)

**MXNet** 

(Amazon)

Developed by U Washington, CMU, MIT, Hong Kong U, etc. but main framework of choice at AWS

PaddlePaddle

(Baidu)

Chainer

(Microsoft)

CNTK

JAX

(Google)







## Recall: Computational Graphs









### The motivation for deep learning frameworks

- 1. Allow rapid prototyping of new ideas
- 2. Automatically compute gradients for you
- 3. Run it all efficiently on GPU or TPU hardware





### For this class we are using **PyTorch version 1.13** (Released October 2022)

Be careful if you are looking at older PyTorch code the API changed a lot before 1.0



### **PyTorch: Versions**



## PyTorch: Version 2.2 (2024)

### further optimize models (torch.compile, scaled dot product attention)

### Intended (not committing) to be backwards compatible









## **PyTorch: Fundamental Concepts**

### **Tensor**: Like a numpy array, but can run on GPU

# Autograd: Package for building computational graphs out of

### Module: A neural network layer; may store state or learnable weights



Tensors, and automatically computing gradients



### Running example: Train a two-layer ReLU network on random data with L2 loss



```
import torch
device = torch.device('cpu')
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D_out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
    y_pred = h_relu.mm(w2)
    loss = (y_pred - y).pow(2).sum()
    grad y pred = 2.0 * (y_pred - y)
    grad_w2 = h_relu.t().mm(grad_y_pred)
    grad_h_relu = grad_y_pred.mm(w2.t())
    grad_h = grad_h_relu.clone()
    grad_h[h < 0] = 0
    grad_w1 = x.t().mm(grad_h)
    w1 -= learning_rate * grad_w1
    w2 -= learning_rate * grad_w2
```



### Create random tensors for data and weights



```
import torch
```

```
device = torch.device('cpu')
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D out, device=device)
```

```
learning_rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
   y_pred = h_relu.mm(w2)
    loss = (y_pred - y).pow(2).sum()
    grad y pred = 2.0 * (y_pred - y)
    grad_w2 = h_relu.t().mm(grad_y_pred)
    grad_h_relu = grad_y_pred.mm(w2.t())
    grad_h = grad_h_relu.clone()
    grad_h[h < 0] = 0
    grad_w1 = x.t().mm(grad_h)
    w1 -= learning_rate * grad_w1
    w2 -= learning_rate * grad_w2
```









```
import torch
device = torch.device('cpu')
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D_out, device=device)
learning_rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
    y_pred = h_relu.mm(w2)
    loss = (y_pred - y).pow(2).sum()
    grad_y_pred = 2.0 * (y_pred - y)
    grad_w2 = h_relu.t().mm(grad_y_pred)
    grad_h_relu = grad_y_pred.mm(w2.t())
    grad_h = grad_h_relu.clone()
    grad_h[h < 0] = 0
    grad_w1 = x.t().mm(grad_h)
    w1 -= learning_rate * grad_w1
    w2 -= learning_rate * grad_w2
```



# Backward pass: manually compute gradients –



```
import torch
device = torch.device('cpu')
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D_out, device=device)
learning_rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
   y_pred = h_relu.mm(w2)
    loss = (y_pred - y).pow(2).sum()
    grad_y_pred = 2.0 * (y_pred - y)
    grad_w2 = h_relu.t().mm(grad_y_pred)
    grad_h_relu = grad_y_pred.mm(w2.t())
    grad_h = grad_h_relu.clone()
    grad_h[h < 0] = 0
    grad_w1 = x.t().mm(grad_h)
```

```
w1 -= learning_rate * grad_w1
w2 -= learning_rate * grad_w2
```



## PyTorch: Tensors

# Gradient descent step on weights



```
import torch
device = torch.device('cpu')
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D_out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
   y_pred = h_relu.mm(w2)
    loss = (y_pred - y).pow(2).sum()
    grad y pred = 2.0 * (y pred - y)
    grad_w2 = h_relu.t().mm(grad_y_pred)
    grad_h_relu = grad_y_pred.mm(w2.t())
    grad_h = grad_h_relu.clone()
    grad_h[h < 0] = 0
    grad_w1 = x.t().mm(grad_h)
    w1 -= learning_rate * grad_w1
```

w2 -= learning rate \* grad w2


#### To run on GPU, just use a different device!



### PyTorch: Tensors

```
import torch
```

```
device = torch.device('cpu')
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D out, device=device)
```

```
learning_rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
   y_pred = h_relu.mm(w2)
    loss = (y_pred - y).pow(2).sum()
    grad_y_pred = 2.0 * (y_pred - y)
    grad_w2 = h_relu.t().mm(grad_y_pred)
    grad_h_relu = grad_y_pred.mm(w2.t())
    grad_h = grad_h_relu.clone()
    grad_h[h < 0] = 0
    grad_w1 = x.t().mm(grad_h)
    w1 -= learning_rate * grad_w1
    w2 -= learning_rate * grad_w2
```



#### Creating Tensors with requires\_grad=True enables autograd

Operations on Tensors with requires\_grad=True cause PyTorch to build a computational graph



```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        w1.grad.zero_()
        w2.grad.zero_()
```



# We will not want gradients (of loss) with respect to data

# Do want gradients with respect to weights



```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero_()
```



#### Compute gradients with respect to all inputs that have requires\_grad=True!



#### import torch

N, D_in, H, D_out = 64, 1000, 100, 10
<pre>x = torch.randn(N, D_in)</pre>
<pre>y = torch.randn(N, D_out)</pre>
<pre>w1 = torch.randn(D_in, H, requires_grad=True)</pre>
<pre>w2 = torch.randn(H, D_out, requires_grad=True)</pre>
<pre>learning_rate = 1e-6</pre>
<pre>for t in range(500):</pre>
<pre>y_pred = x.mm(w1).clamp(min=0).mm(w2)</pre>
<pre>loss = (y_pred - y).pow(2).sum()</pre>

loss.backward()

```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    w1.grad.zero_()
    w2.grad.zero_()
```





#### Every operation on a tensor with requires\_grad=True will add to the computational graph, and the resulting tensors will also have requires\_grad=True



```
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
   y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
   with torch.no_grad():
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```





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```
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero_()
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```
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w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
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w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        w1.grad.zero_()
        w2.grad.zero_()
```







```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        w1.grad.zero_()
        w2.grad.zero_()
```







```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        w1.grad.zero_()
        w2.grad.zero_()
```









#### After backward finishes, gradients are accumulated into w1.grad and w2.grad and the graph is destroyed



#### import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    w1.grad.zero_()
    w2.grad.zero_()
```





#### After backward finishes, gradients are accumulated into w1.grad and w2.grad and the graph is destroyed

Make gradient step on weights



#### import torch

	N, D_in, H, D_out = 64, 1000, 100, 10					
	<pre>x = torch.randn(N, D_in)</pre>					
	<pre>y = torch.randn(N, D_out)</pre>					
	<pre>w1 = torch.randn(D_in, H, requires_grad=True) w2 = torch.randn(H, D_out, requires_grad=True)</pre>					
	<pre>learning_rate = 1e-6</pre>					
	<pre>for t in range(500):     y_pred = x.mm(w1).clamp(min=0).mm(w2)     loss = (y_pred - y).pow(2).sum()</pre>					

loss.backward()

```
with torch.no_grad():
w1 -= learning_rate * w1.grad
w2 -= learning rate * w2.grad
w1.grad.zero_()
w2.grad.zero_()
```





#### After backward finishes, gradients are accumulated into w1.grad and w2.grad and the graph is destroyed

Set gradients to zero—forgetting this is a common bug!









#### After backward finishes, gradients are accumulated into w1.grad and w2.grad and the graph is destroyed

Tell PyTorch not to build a graph for these operations



#### import torch

N, D_in, H, D_out = 64, 1000, 100, 10					
<pre>x = torch.randn(N, D_in)</pre>					
<pre>y = torch.randn(N, D_out)</pre>					
<pre>w1 = torch.randn(D_in, H, requires_grad=True)</pre>					
<pre>w2 = torch.randn(H, D_out, requires_grad=True)</pre>					
learning_rate = 1e-6					
<pre>for t in range(500):</pre>					
<pre>y_pred = x.mm(w1).clamp(min=0).mm(w2)</pre>					
<pre>loss = (y_pred - y).pow(2).sum()</pre>					

loss.backward()

```
with torch.no_grad():
```

w1 -=	learning_rate	*	w1.grad			
w2 -=	learning_rate	*	w2.grad			
w1.grad.zero_()						
w2.grad.zero_()						



Can define new operations using Python functions

def sigmoid(x):
 return 1.0 / (1.0 + (-x).exp())



```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
y = torch.randn(N, D_out)
w1 = torch.randn(D in, H, requires_grad=True)
w2 = torch.randn(H, D out, requires grad=True)
learning_rate = 1e-6
for t in range(500):
  y_pred = sigmoid(x.mm(w1)).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  loss.backward()
  if t % 50 == 0:
   print(t, loss.item())
  with torch.no_grad():
    w1 -= learning_rate * w1.grad
   w2 -= learning_rate * w2.grad
    wl.grad.zero ()
    w2.grad.zero ()
```



Can define new operations using Python functions

def sigmoid(x):
 return 1.0 / (1.0 + (-x).exp())





```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D out, requires grad=True)
learning_rate = 1e-6
for t in range(500):
  y_pred = sigmoid(x.mm(w1)).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  loss.backward()
  if t % 50 == 0:
    print(t, loss.item())
  with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    wl.grad.zero ()
    w2.grad.zero ()
```



Can define new operations using Python functions

def sigmoid(x):
 return 1.0 / (1.0 + (-x).exp())





Define new autograd operators by subclassing Function, define forward and backward

```
class Sigmoid(torch.autograd.Function):
     @staticmethod
    def forward(ctx, x):
       y = 1.0 / (1.0 + (-x).exp())
       ctx.save_for_backward(y)
       return y
     @staticmethod
    def backward(ctx, grad_y):
       y, = ctx.saved_tensors
       grad x = grad y * y * (1.0 - y)
       return grad x
  def sigmoid(x):
    return Sigmoid.apply(x)
Recall: \frac{\partial}{\partial x} \left[ \sigma(x) \right] = (1 - \sigma(x)) \sigma(x)
```

54



Can define new operations using Python functions

def sigmoid(x):
 return 1.0 / (1.0 + (-x).exp())





Define new autograd operators by subclassing Function, define forward and backward

```
class Sigmoid(torch.autograd.Function):
    @staticmethod
    def forward(ctx, x):
        y = 1.0 / (1.0 + (-x).exp())
        ctx.save_for_backward(y)
        return y
    @staticmethod
    def backward(ctx, grad_y):
        y, = ctx.saved_tensors
        grad_x = grad_y * y * (1.0 - y)
        return grad_x
def sigmoid(x):
    return Sigmoid.apply(x)
```

Now when our function runs, it adds one node to the graph!





Can define new operations using Python functions

def sigmoid(x):
 return 1.0 / (1.0 + (-x).exp())





Define new autograd operators by subclassing Function, define forward and backward

```
class Sigmoid(torch.autograd.Function):
    @staticmethod
    def forward(ctx, x):
        y = 1.0 / (1.0 + (-x).exp())
        ctx.save_for_backward(y)
        return y
    @staticmethod
    def backward(ctx, grad_y):
        y, = ctx.saved_tensors
        grad_x = grad_y * y * (1.0 - y)
        return grad_x
def sigmoid(x):
    return Sigmoid.apply(x)
```

In practice this is pretty rare – in most cases Python functions are good enough



#### Higher-level wrapper for working with neural nets

#### Use this! It will make your life easier



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D_out))
learning_rate = 1e-2
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    with torch.no_grad():
        for param in model.parameters():
            param -= learning rate * param.grad
    model.zero grad()
```



#### **Object-oriented API: Define** model object as sequence of layers objects, each of which holds weight tensors



```
import torch
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
```

```
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
```

```
learning_rate = 1e-2
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    with torch.no_grad():
        for param in model.parameters():
            param -= learning_rate * param.grad
    model.zero_grad()
```





#### Forward pass: Feed data to model and compute loss



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D_out))
learning_rate = 1e-2
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    with torch.no_grad():
        for param in model.parameters():
            param -= learning_rate * param.grad
    model.zero grad()
```





#### Forward pass: Feed data to model and compute loss

torch.nn.functional has useful helpers like loss functions



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D_out))
learning_rate = 1e-2
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    with torch.no_grad():
        for param in model.parameters():
            param -= learning_rate * param.grad
    model.zero_grad()
```





#### Backward pass: compute gradient with respect to all model weights (they have requires\_grad=True)



### PyTorch: nn

```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D_out))
learning_rate = 1e-2
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
```

loss.backward()

```
with torch.no_grad():
    for param in model.parameters():
        param -= learning_rate * param.grad
model.zero_grad()
```





#### Make gradient step on each model parameter (with gradients disabled)



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D_out))
learning_rate = 1e-2
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    with torch.no_grad():
        for param in model.parameters():
            param -= learning_rate * param.grad
    model.zero grad()
```



### PyTorch: optim

## Use an **optimizer** for different update rules



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D_out))
learning rate = 1e-4
optimizer = torch.optim.Adam(model.parameters(),
                              lr=learning_rate)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```



## PyTorch: optim

#### After computing gradients, use optimizer to update and zero gradients



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning_rate = 1e-4
optimizer = torch.optim.Adam(model.parameters(),
                              lr=learning_rate)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
```

optimizer.zero grad()



# A PyTorch **Module** is a neural net layer; it inputs and outputs Tensors

Modules can contain weights or other modules

Very common to define your own models or layers as custom Modules



```
import torch
class TwoLayerNet(torch.nn.Module):
    def __init__(self, D_in, H, D_out):
        super(TwoLayerNet, self).__init__()
        self.linear1 = torch.nn.Linear(D in, H)
        self.linear2 = torch.nn.Linear(H, D out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y pred = self.linear2(h relu)
        return y pred
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = TwoLayerNet(D_in, H, D_out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()
```



# Define our whole model as a single Module



```
import torch
class TwoLayerNet(torch.nn.Module):
    def __init__(self, D_in, H, D_out):
        super(TwoLayerNet, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, H)
        self.linear2 = torch.nn.Linear(H, D_out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y_pred = self.linear2(h_relu)
        return y pred
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
model = TwoLayerNet(D_in, H, D_out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y_{pred} = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()
```



#### Initializer sets up two children (Modules can contain modules)



### PyTorch: nn **Defining Modules**

```
import torch
class TwoLayerNet(torch.nn.Module):
    def __init__(self, D_in, H, D_out):
        super(TwoLayerNet, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, H)
        self.linear2 = torch.nn.Linear(H, D out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y pred = self.linear2(h relu)
        return y pred
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = TwoLayerNet(D_in, H, D_out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()
```



#### Define forward pass using child modules and tensor operations

No need to define backward autograd will handle it



#### PyTorch: nn **Defining Modules**

```
import torch
class TwoLayerNet(torch.nn.Module):
    def __init__(self, D_in, H, D_out):
        super(TwoLayerNet, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, H)
        self.linear2 = torch.nn.Linear(H, D out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y_pred = self.linear2(h relu)
        return y_pred
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = TwoLayerNet(D_in, H, D_out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()
```



#### Very common to mix and match custom Module subclasses and Sequential containers



```
import torch
class ParallelBlock(torch.nn.Module):
    def __init__(self, D_in, D_out):
        super(ParallelBlock, self). init ()
        self.linear1 = torch.nn.Linear(D in, D out)
        self.linear2 = torch.nn.Linear(D in, D out)
    def forward(self, x):
        h1 = self.linear1(x)
        h2 = self.linear2(x)
        return (h1 * h2).clamp(min=0)
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
            ParallelBlock(D_in, H),
            ParallelBlock(H, H),
            torch.nn.Linear(H, D_out))
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()
```



#### Define network component as a Module subclass





```
import torch
class ParallelBlock(torch.nn.Module):
    def __init__(self, D_in, D_out):
        super(ParallelBlock, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, D_out)
        self.linear2 = torch.nn.Linear(D in, D out)
    def forward(self, x):
        h1 = self.linear1(x)
        h2 = self.linear2(x)
        return (h1 * h2).clamp(min=0)
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
            ParallelBlock(D_in, H),
            ParallelBlock(H, H),
            torch.nn.Linear(H, D_out))
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()
```



# Stack multiple instances of the component in a sequential

Very easy to quickly build complex network architectures!





```
import torch
class ParallelBlock(torch.nn.Module):
    def init (self, D in, D out):
        super(ParallelBlock, self). init ()
        self.linear1 = torch.nn.Linear(D in, D out)
        self.linear2 = torch.nn.Linear(D in, D out)
    def forward(self, x):
        h1 = self.linear1(x)
        h2 = self.linear2(x)
        return (h1 * h2).clamp(min=0)
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
 = torch.randn(N, D out)
model = torch.nn.Sequential(
            ParallelBlock(D in, H),
            ParallelBlock(H, H),
            torch.nn.Linear(H, D_out))
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()
```



A **DataLoader** wraps a **Dataset** and provides minibatching, shuffling, multithreading, for you

When you need to load custom data, just write your own Dataset class

import torch



### PyTorch: DataLoaders

```
from torch.utils.data import TensorDataset, DataLoader
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
loader = DataLoader(TensorDataset(x, y), batch_size=8)
model = TwoLayerNet(D_in, H, D_out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-2)
for epoch in range(20):
    for x_batch, y_batch in loader:
        y_pred = model(x_batch)
        loss = torch.nn.functional.mse_loss(y_pred, y_batch)
        loss.backward()
        optimizer.step()
        optimizer.zero_grad()
```




#### Iterate over loader to form minibatches



### PyTorch: DataLoaders

```
from torch.utils.data import TensorDataset, DataLoader
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
loader = DataLoader(TensorDataset(x, y), batch_size=8)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-2)
for epoch in range(20):
    for x_batch, y_batch in loader:
        y_pred = model(x_batch)
        loss = torch.nn.functional.mse_loss(y_pred, y_batch)
        loss.backward()
        optimizer.step()
```

```
optimizer.zero_grad()
```



## PyTorch: Pretrained Models

Super easy to use pertained models with torch vision

https://pytorch.org/vision/stable/

import torch
import torchvision

alexnet = torchvision.models.alexnet(pretrained=True)
vgg16 = torchvision.models.vgg16(pretrained=True)
resnet101 = torchvision.models.resnet101(pretrained=True)







```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```







import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

#### **Create Tensor objects**







```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

```
loss.backward()
```

Build graph data structure AND perform computation







```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

```
loss.backward()
```

Build graph data structure AND perform computation







```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

Perform backprop, throw away graph



### x w1 w2 y



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

Perform backprop, throw away graph







```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

```
loss.backward()
```

Build graph data structure AND perform computation







```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

```
loss.backward()
```

Build graph data structure AND perform computation







```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

Perform backprop, throw away graph



Dynamic graphs let you use regular Python control flow during the forward pass!



```
import torch
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
prev_loss = 5.0
for t in range(500):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  loss.backward()
  prev loss = loss.item()
```



Dynamic graphs let you use regular Python control flow during the forward pass!

Initialize two different weight matrices for second layer



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
prev_loss = 5.0
for t in range(500):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  loss.backward()</pre>
```

```
prev_loss = loss.item()
```



Dynamic graphs let you use regular Python control flow during the forward pass!

Decide which one to use at each layer based on loss at previous iteration

(this model doesn't makes sense! Just a simple dynamic example)



```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
prev_loss = 5.0
for t in range(500):
w2 = w2a if prev loss < 5.0 else w2b
y_pred = x.mm(w1).clamp(min=0).mm(w2)
loss = (y_pred - y).pow(2).sum()
loss.backward()
prev loss = loss.item()
```



### Alternative: Static Computation Graphs

Alternative: Static graphs

Step 1: Build computational graph describing our computation (including finding paths for backprop)

Step 2: Reuse the same graph on every iteration

DeepRob

g e



- graph = build\_graph()
- for x\_batch, y\_batch in loader:
   run\_graph(graph, x=x\_batch, y=y\_batch)



Define model as a Python function



#### import torch

<pre>def model(x, y, w1, w2a, w2b, prev_loss):   w2 = w2a if prev_loss &lt; 5.0 else w2b   y_pred = x.mm(w1).clamp(min=0).mm(w2)   loss = (y_pred - y).pow(2).sum()   return loss</pre>	
<pre>N, D_in, H, D_out = 64, 1000, 100, 10 x = torch.randn(N, D_in) y = torch.randn(N, D_out) w1 = torch.randn(D_in, H, requires_grad=True) w2a = torch.randn(H, D_out, requires_grad=True) w2b = torch.randn(H, D_out, requires_grad=True)</pre>	1e) 1e)
<pre>graph = torch.jit.script(model)</pre>	
<pre>prev_loss = 5.0 learning_rate = 1e-6 for t in range(500):    loss = graph(x, y, w1, w2a, w2b, prev_loss)</pre>	)_
<pre>loss.backward() prev loss = loss.item()</pre>	



Just-In-Time compilation: Introspect the source code of the function, **compile** it into a graph object.

Lots of magic here!



#### import torch

```
def model(x, y, w1, w2a, w2b, prev_loss):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  return loss
N, D_in, H, D_out = 64, 1000, 100, 10
  x = torch.randn(N, D_in)
  y = torch.randn(N, D_out)
w1 = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
```

graph = torch.jit.script(model)

```
prev_loss = 5.0
learning_rate = 1e-6
for t in range(500):
   loss = graph(x, y, w1, w2a, w2b, prev_loss)
   loss.backward()
   prev_loss = loss.item()
```





#### import torch

```
def model(x, y, w1, w2a, w2b, prev_loss):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  return loss
N, D_in, H, D_out = 64, 1000, 100, 10
  x = torch.randn(N, D_in)
  y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
```

graph = torch.jit.script(model)

```
prev_loss = 5.0
learning_rate = 1e-6
for t in range(500):
  loss = graph(x, y, w1, w2a, w2b, prev_loss)
  loss.backward()
  prev_loss = loss.item()
```



### Use our compiled graph object at each forward pass



#### import torch

```
def model(x, y, w1, w2a, w2b, prev loss):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  return loss
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
graph = torch.jit.script(model)
prev loss = 5.0
learning_rate = 1e-6
for t in range(500):
 loss = graph<u>(</u>x, y, w1, w2a, w2b, prev_loss<u>)</u>
```

```
loss.backward()
prev_loss = loss.item()
```



Even easier: add **annotation** to function, Python function compiled to a graph when it is defined

Calling function uses graph



#### import torch

```
@torch.jit.script
def model(x, y, w1, w2a, w2b, prev_loss):
  w2 = w2a if prev_loss < 5.0 else w2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  return loss
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D out, requires grad=True)
prev loss = 5.0
learning rate = 1e-6
for t in range(500):
  loss = model(x, y, w1, w2a, w2b, prev_loss)
 loss.backward()
  prev loss = loss.item()
```



## Static vs Dynamic Graphs: Optimization

With static graphs, framework can **optimize** the graph for you before it runs! The graph you wrote





Conv ReLU ReLU ReLU

Conv

ReLU

Equivalent graph with fused operations

Conv+ReLU

Conv+ReLU

Conv+ReLU



## Static vs Dynamic Graphs: Optimization

### Static

Once graph is built, can serialize it and run it without the code that built the graph!

e.g. train model in Python, deploy in C++



### Dynamic

Graph building and execution are intertwined, so always need to keep code around



## Static vs Dynamic Graphs: Optimization

### Static

Lots of indirection between the code you write and the code that runs – can be hard to debug, benchmark, etc



### Dynamic

The code you write is the code that runs! Easy to reason about, debug, profile, etc



## **Dynamic Graph Applications**

### Model structure depends on the input:

- Recurrent Networks
- Recursive Networks



DEED Report Neural Networks, Divyam Rastogi, Oliver Brock. "Differentiable Particle Filters: End-to-End Learning with Algorithmic Priors" RSS, 2018 In the secure of the s





## Dynamic Graph Applications

# Model structure depends on the input:

- Recurrent Networks
- Recursive Networks
- Modular Networks





## Dynamic Graph Applications

# Model structure depends on the input:

- Recurrent Networks
- Recursive Networks
- Modular Networks
- (Your idea here!)



### **Final Project**



### TensorFlow: Versions

### TensorFlow 1.0

- Final release: 1.15.3
- Default: static graphs
- Optional: dynamic graphs (eager mode)



### TensorFlow 2.0

- Current release: 2.8.0
  Released 2/2/2022
- Default: dynamic graphs
- Optional: static graphs



### TensorFlow 1.0: Static Graphs

### import numpy as np import tensorflow as tf

## (Assume imports at the top of each snippet)



```
N, D, H = 64, 1000, 100
x = tf.placeholder(tf.float32, shape=(N, D))
y = tf.placeholder(tf.float32, shape=(N, D))
w1 = tf.placeholder(tf.float32, shape=(D, H))
w2 = tf.placeholder(tf.float32, shape=(H, D))
h = tf.maximum(tf.matmul(x, w1), 0)
y_pred = tf.matmul(h, w2)
diff = y pred - y
loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
grad_w1, grad_w2 = tf.gradients(loss, [w1, w2])
with tf.Session() as sess:
    values = {x: np.random.randn(N, D),
              wl: np.random.randn(D, H),
              w2: np.random.randn(H, D),
              y: np.random.randn(N, D),}
    out = sess.run([loss, grad_w1, grad_w2],
                   feed dict=values)
    loss_val, grad_wl_val, grad_w2_val = out
```





### TensorFlow 1.0: Static Graphs

### First **define** computational graph

### Then **run** the graph many times



```
N, D, H = 64, 1000, 100
x = tf.placeholder(tf.float32, shape=(N, D))
y = tf.placeholder(tf.float32, shape=(N, D))
w1 = tf.placeholder(tf.float32, shape=(D, H))
w2 = tf.placeholder(tf.float32, shape=(H, D))
h = tf.maximum(tf.matmul(x, wl), 0)
y_pred = tf.matmul(h, w2)
diff = y pred - y
loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
grad_w1, grad_w2 = tf.gradients(loss, [w1, w2])
```

```
with tf.Session() as sess:
    values = {x: np.random.randn(N, D),
              wl: np.random.randn(D, H),
              w2: np.random.randn(H, D),
              y: np.random.randn(N, D),}
    out = sess.run([loss, grad_w1, grad_w2],
                   feed dict=values)
    loss_val, grad_wl_val, grad_w2_val = out
```







Create TensorFlow Tensors for data and weights

Weights need to be wrapped in tf.Variable so we can mutate them



```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
```

```
learning rate = 1e-6
for t in range(1000):
 with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
   y_pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
  grad_w1, grad_w2 = tape.gradient(loss, [w1, w2])
 w1.assign(w1 - learning_rate * grad_w1)
 w2.assign(w2 - learning_rate * grad_w2)
```







Scope forward pass under a GradientTape to tell TensorFlow to start building a graph



```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
   h = tf.maximum(tf.matmul(x, w1), 0)
   y pred = tf.matmul(h, w2)
   diff = y pred - y
   loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
  grad_w1, grad_w2 = tape.gradient(loss, [w1, w2])
 w1.assign(w1 - learning rate * grad w1)
 w2.assign(w2 - learning_rate * grad_w2)
```





Scope forward pass under a GradientTape to tell TensorFlow to start building a graph

> In PyTorch, all ops build graph by default; **opt out** via torch.no\_grad In Tensorflow, ops do not build graph by default; opt in via GradientTape



```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
   h = tf.maximum(tf.matmul(x, w1), 0)
   y pred = tf.matmul(h, w2)
   diff = y pred - y
   loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
  grad_w1, grad_w2 = tape.gradient(loss, [w1, w2])
 w1.assign(w1 - learning rate * grad w1)
 w2.assign(w2 - learning_rate * grad_w2)
```





### Ask the tape to compute gradients



```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y_pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning_rate * grad_w1)
  w2.assign(w2 - learning rate * grad w2)
```





Gradient descent step, update weights





```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
 with tf.GradientTape() as tape:
   h = tf.maximum(tf.matmul(x, w1), 0)
   y_pred = tf.matmul(h, w2)
   diff = y pred - y
    loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
  grad_w1, grad_w2 = tape.gradient(loss, [w1, w2])
 w1.assign(w1 - learning_rate * grad_w1)
  w2.assign(w2 - learning rate * grad w2)
```





### TensorFlow 2.0: Static Graphs

Define a function that implements forward, backward, and update

Annotating with tf.function will compile the function into a graph! (similar to torch.jit.script)



```
@tf.function
def step(x, y, w1, w2):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
  grad_w1, grad_w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning_rate * grad_w2)
  return loss
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning_rate = 1e-6
for t in range(1000):
  loss = step(x, y, w1, w2)
```





## TensorFlow 2.0: Static Graphs

Define a function that implements forward, backward, and update

Annotating with tf.function will compile the function into a graph! (similar to torch.jit.script)

(note TF graph can include gradient computation and update, unlike PyTorch)



```
@tf.function
def step(x, y, w1, w2):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
 return loss
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning_rate = 1e-6
for t in range(1000):
  loss = step(x, y, w1, w2)
```




#### TensorFlow 2.0: Static Graphs

Call the compiled step function in the training loop



```
@tf.function
def step(x, y, w1, w2):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y_pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
  grad_w1, grad_w2 = tape.gradient(loss, [w1, w2])
 w1.assign(w1 - learning_rate * grad_w1)
 w2.assign(w2 - learning rate * grad w2)
  return loss
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
```

```
loss = step(x, y, w1, w2)
```







```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning_rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y \text{ pred} = \text{model}(x)
    loss = loss fn(y pred, y)
  grads = tape.gradient(loss, params)
  opt.apply_gradients(zip(grads, params))
```



Object-oriented API: build the model as a stack of layers



import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense

```
N, Din, H, Dout = 16, 1000, 100, 10
```

```
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable_variables
```

```
loss_fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning_rate=1e-6)
```

```
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
```

```
for t in range(1000):
    with tf.GradientTape() as tape:
        y_pred = model(x)
        loss = loss_fn(y_pred, y)
        grads = tape.gradient(loss, params)
        opt.apply_gradients(zip(grads, params))
```



Keras gives you common loss functions and optimization algorithms



```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y \text{ pred} = \text{model}(x)
    loss = loss fn(y pred, y)
  grads = tape.gradient(loss, params)
  opt.apply_gradients(zip(grads, params))
```



Forward pass: Compute loss, build graph



Backward pass: compute gradients



```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning_rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y \text{ pred} = \text{model}(x)
    loss = loss fn(y pred, y)
  grads = tape.gradient(loss, params)
  opt.apply_gradients(zip(grads, params))
```



Optimizer object updates parameters





```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning_rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y \text{ pred} = \text{model}(x)
    loss = loss fn(y pred, y)
  grads = tape.gradient(loss, params)
  opt.apply_gradients(zip(grads, params))
```



Define a function that returns the loss





```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
def step():
  y_{pred} = model(x)
  loss = loss fn(y pred, y)
  return loss
for t in range(1000):
  opt.minimize(step, params)
```



Optimizer computes gradients and updates parameters





```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
def step():
  y_{pred} = model(x)
  loss = loss_fn(y_pred, y)
  return loss
for t in range(1000):
  opt.minimize(step, params)
```





TensorBoard					
Regex filter	×	loss			
Split on underscores		loss			
Data download links		120 -			
Horizontal Axis		80.0			
STEP RELATIVE WALL		40.0			
		0.00			
Runs		53	0.000	20.00	4(
✓ .					



#### TensorBoard







# Summary: PyTorch vs TensorFlow

#### Pytorch

- Clean, imperative API
- **Dynamic** graphs for easy debugging
- JIT allows static graphs for production
- Hard/inefficient to use on TPUs
- Not easy to deploy on mobile
- API could be messy
- Tensorflow 2.0: dynamic by default; standardized on Keras API



#### • Tensorflow 1.0: static graphs by default; can be confusing to debug;





#### Lecture 12 **Deep Learning Software University of Michigan I Department of Robotics**



